

# Sharp imaging of Multiple object pointS: How and Why

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L. Jiayao<sup>1</sup>, J.M. Infante<sup>1</sup>, F. Duerr<sup>3</sup>

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<sup>3</sup>VUB, Belgium



# Abstract:

- Is it possible to sharply image  $M$  object points with  $N$  surfaces when  $N < M$ ?
- Under what conditions?
- Why is it interesting for optimization?
- What is the role of the SMS method?

Answers will be given!



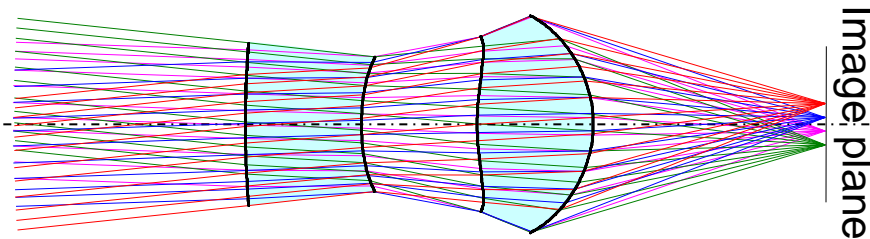
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# SMS method

Usually presented as a method to couple N wavefront pairs with N surfaces

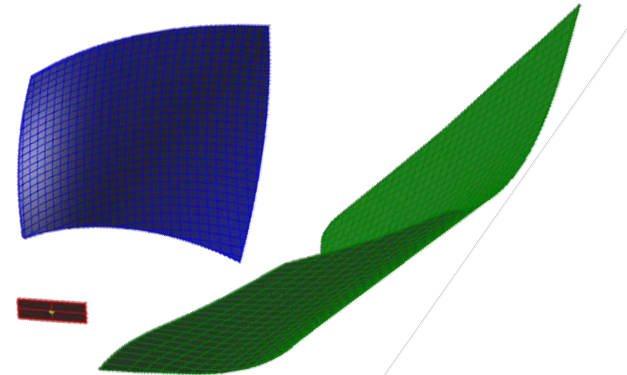
## SMS 2D



Up to ~~6~~ aspheres

J.C. Miñano et al., Optics Express, Volume 17, 2009

## SMS 3D



Up to 2 free-forms

P. Benítez et al., Optical Engineering, 2003



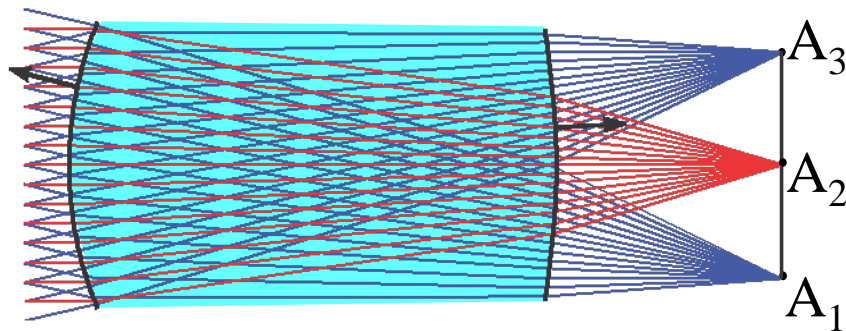
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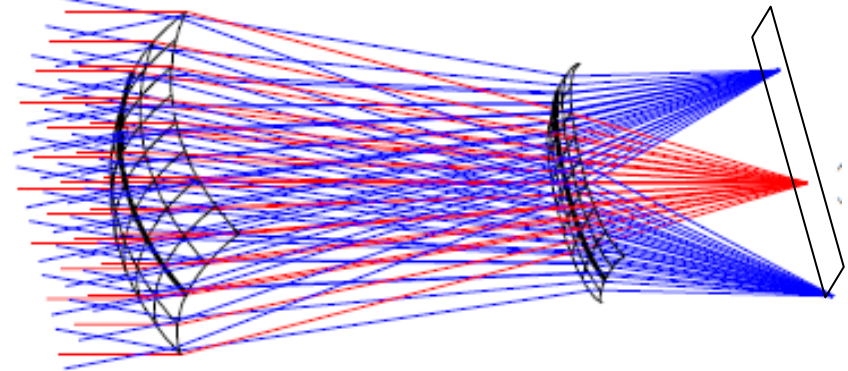
# SMS method

However, recent findings seem contradictory

SMS 2D



SMS 3D



F. Duerr, P. Benítez, J.C. Miñano, Y. Meuret, H. Thienpont, Opt.Express 20, 5576–5585, (2012)

F. Duerr, P. Benítez, J.C. Miñano, Y. Meuret, H. Thienpont, Optics Express 20, 10839–10846, (2012)

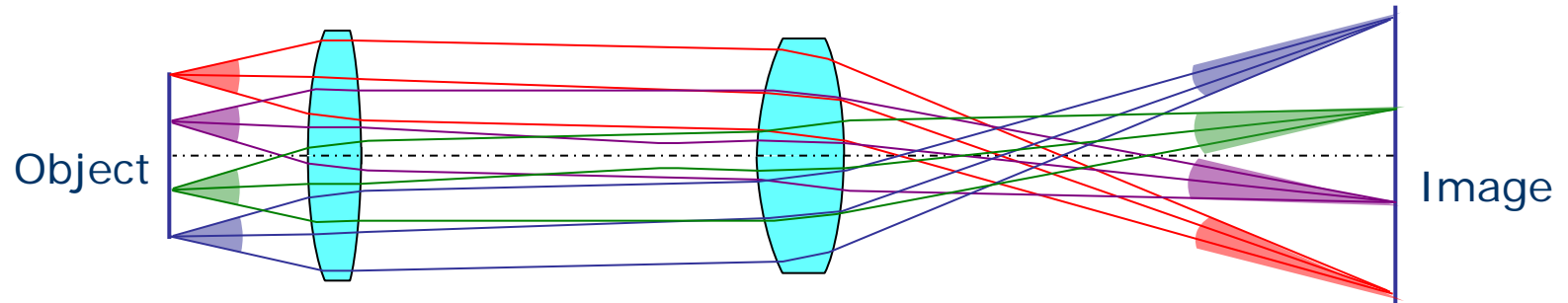


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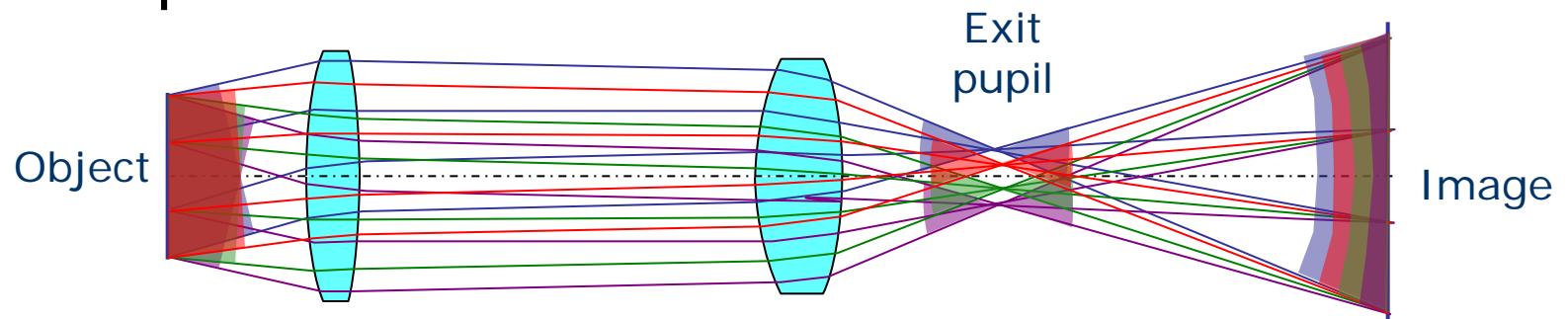


# Object versus Pupil discretization

- Object discretization



- Pupil discretization



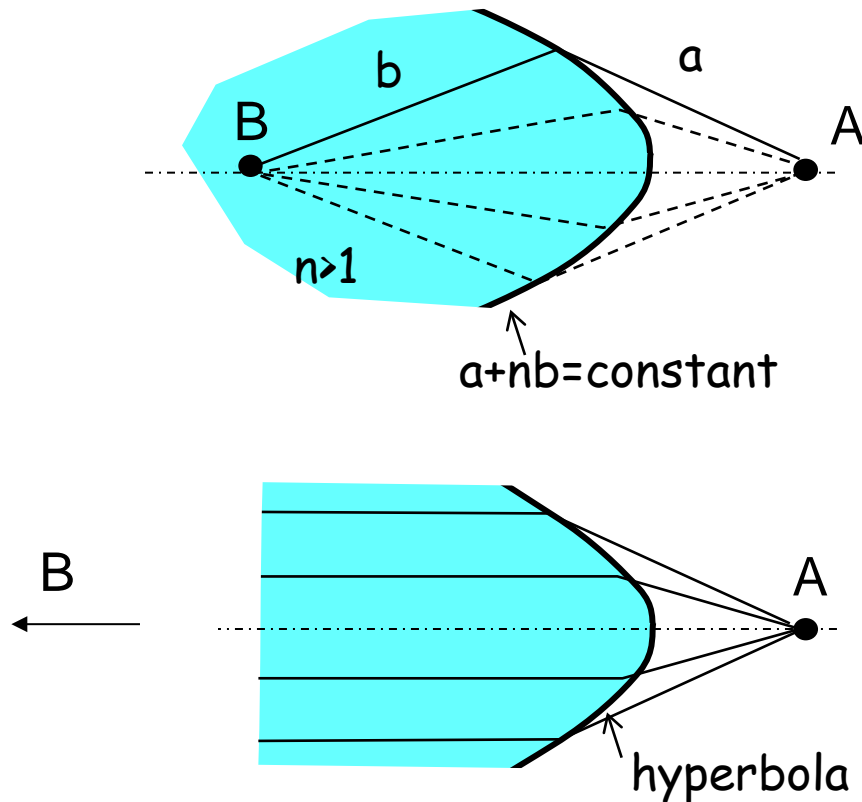
# Index

- Let's start simple
- Facing the general case
- Application to optimization
- Conclusions



# Early work

## Cartesian ovals



R. Descartes, "Géométrie",  
Leyden (1637)

These are 2D and 3D solutions



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# Early work

## On the problem of ideal flux concentrators

**W. T. Welford**

*Blackett Laboratory, Imperial College, London SW7 2BZ, United Kingdom*

**R. Winston**

*Enrico Fermi Institute and Department of Physics, University of Chicago, Chicago, Illinois 60637*

*(Received 28 September 1977)*



one of these for rays incident above the axis and the other for rays incident below the axis, and this is impossible. Thus in general it is not possible to correct a system with a finite number of surfaces for meridian rays to one off-axis object point, much less for skew rays. There are well-known exceptions to this, namely, systems of spherical symmetry such

(1977)



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# Early work

## On the problem of ideal flux concentrators: Addendum

W. T. Welford

*Blackett Laboratory, Imperial College, London SW7 2BZ, United Kingdom*

R. Winston

*Enrico Fermi Institute and Department of Physics, University of Chicago, Chicago, Illinois 60637*

*(Received 13 September 1978; revised 3 November 1978)*



and so on. But we have only a finite number  $n$  of surfaces available, so that only  $n - 1$  one-dimensional fans of rays can come to a point focus, not the full two-dimensional array in the pupil.

(1978)

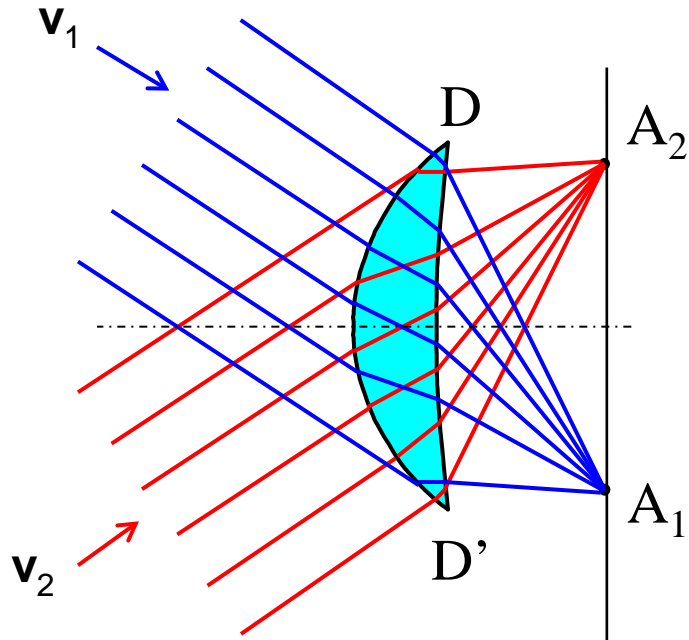


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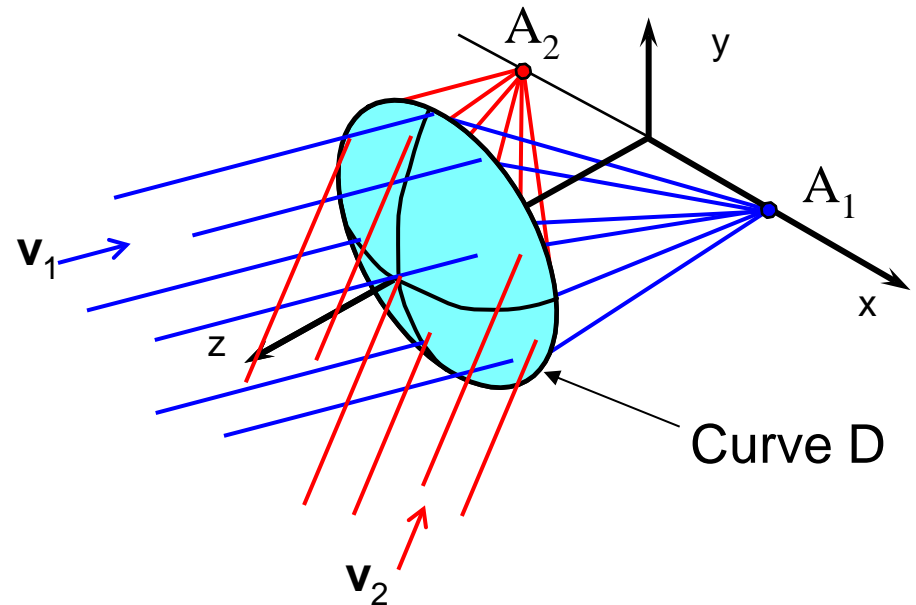
# First SMS designs

In 2D



J.C. Miñano, J.C. Glez,  
Appl. Opt. 31 (16), 1992

In 3D



P. Benítez, R. Mohedano, J.C. Miñano,  
SPIE Vol. 3781, 1999

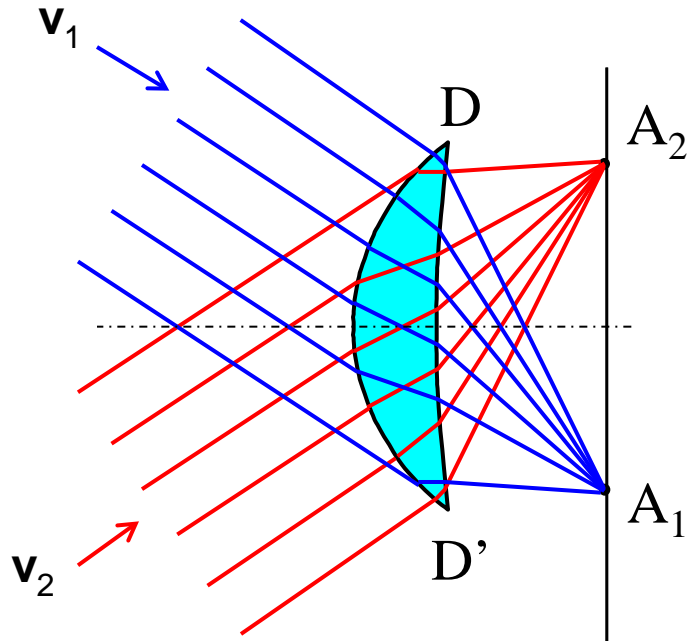


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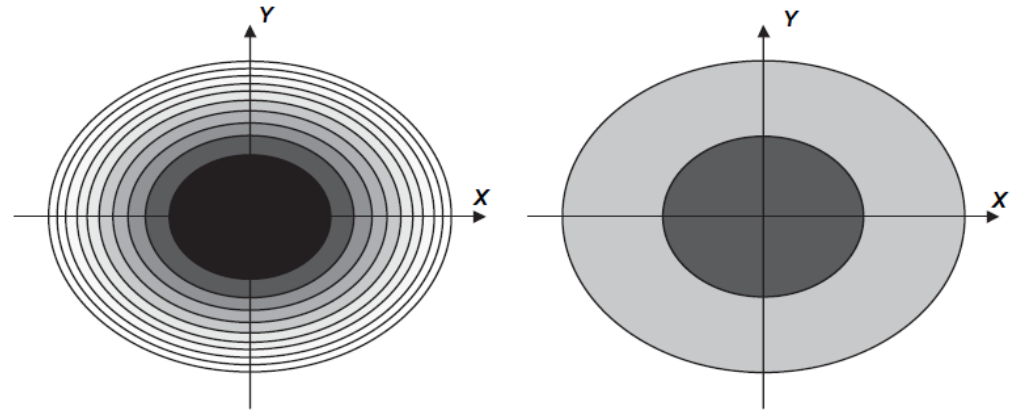
# First SMS designs

In 2D



J.C. Miñano, J.C. Glez,  
Appl. Opt. 31 (16), 1992

In 3D



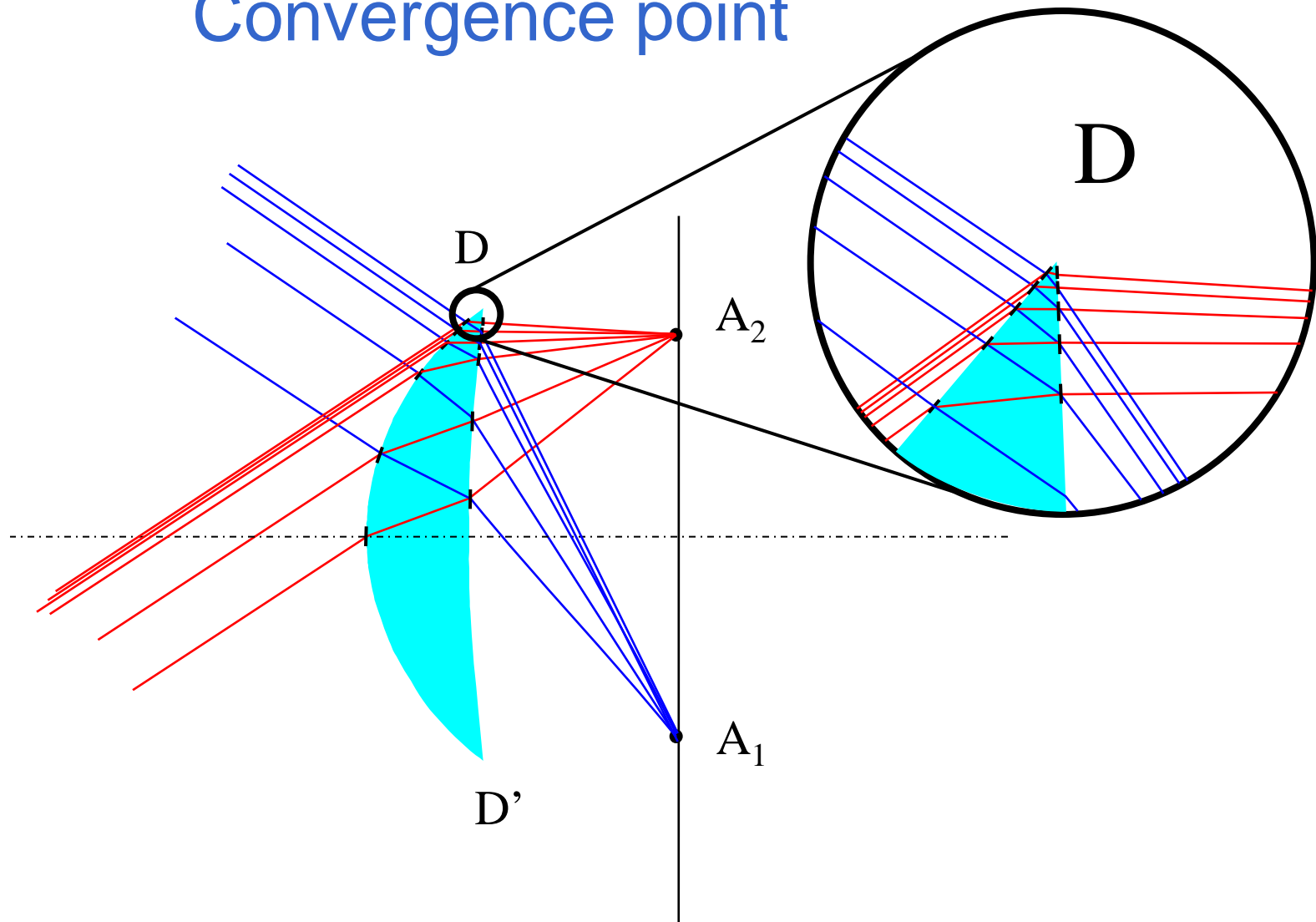
P. Benítez, R. Mohedano, J.C. Miñano,  
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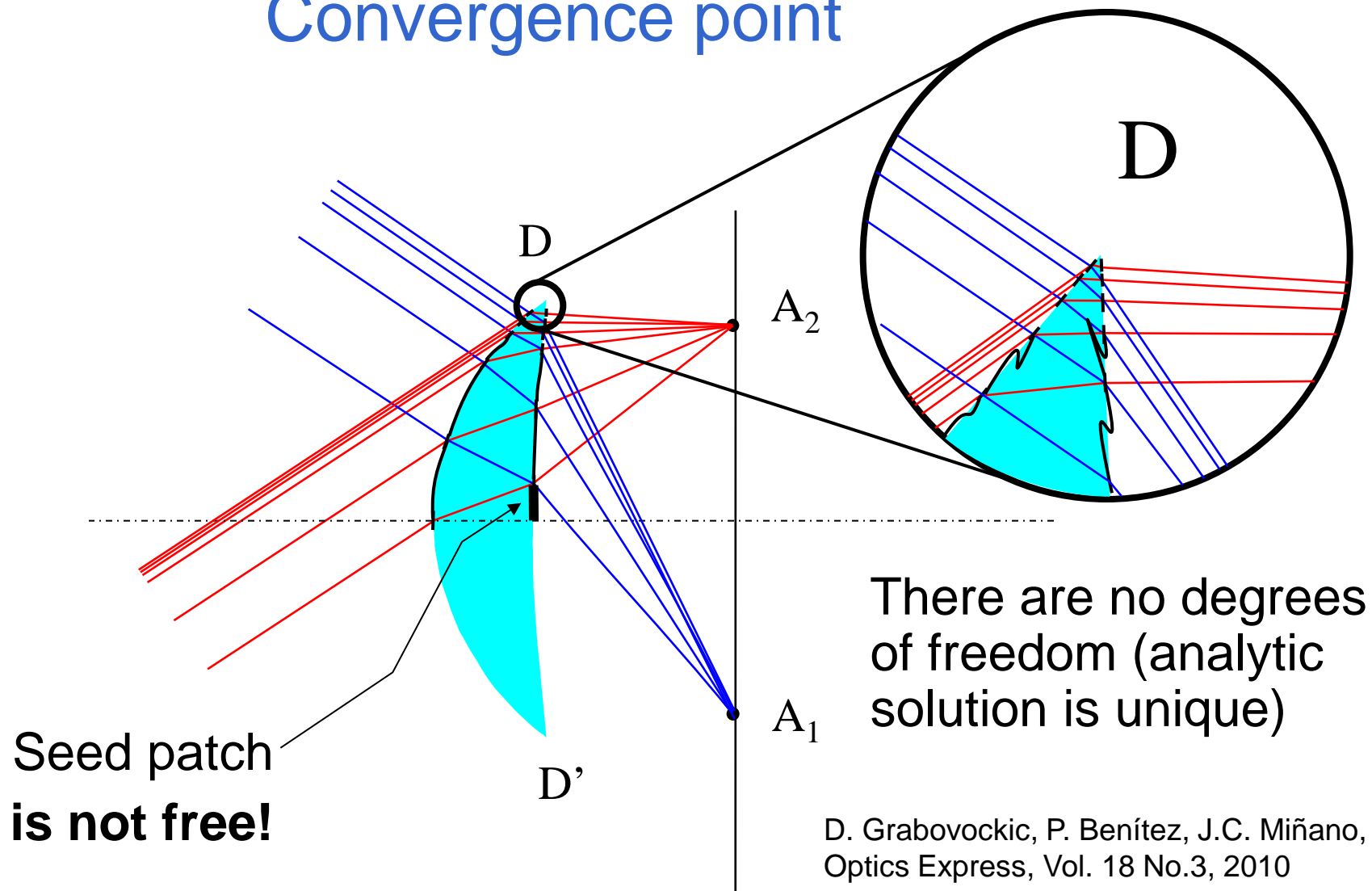
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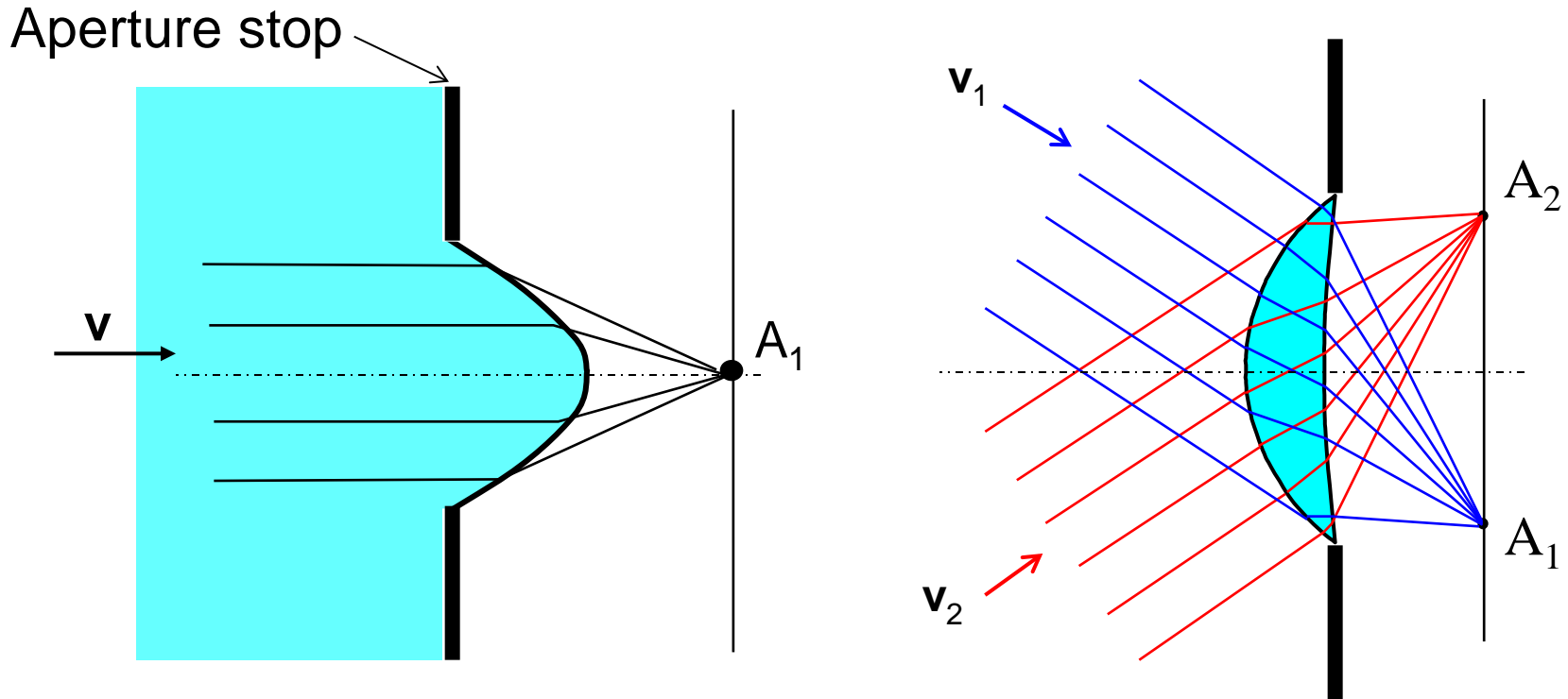
# Convergence point



# Convergence point

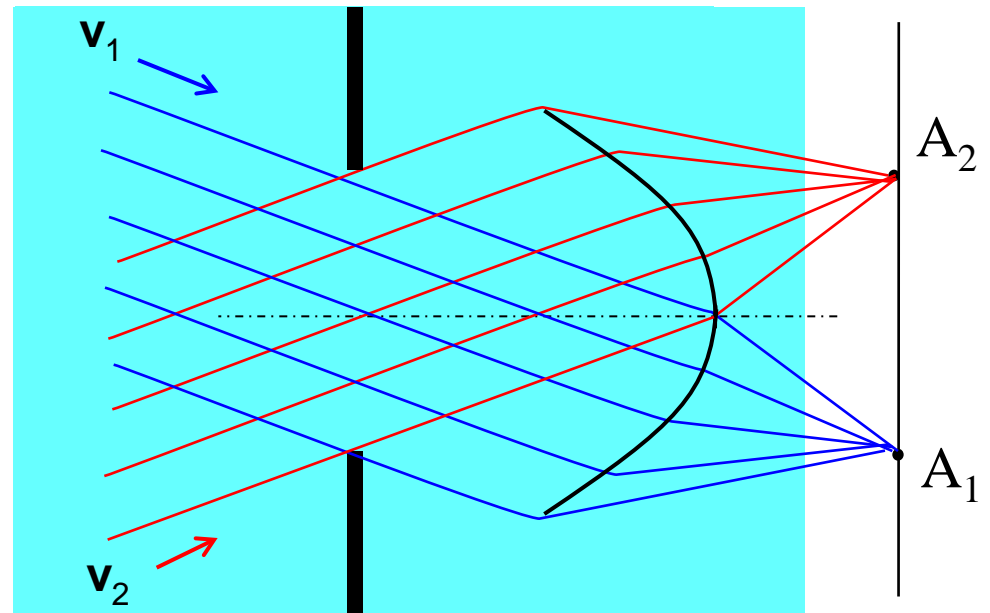
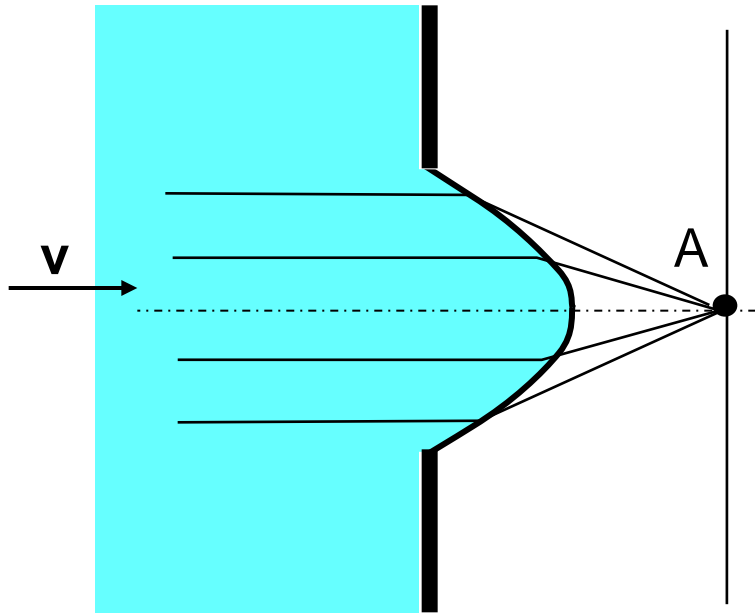


# Similarities



- All surfaces are at the aperture stop
- Both are unique solutions
- Number of object points = Number of surfaces

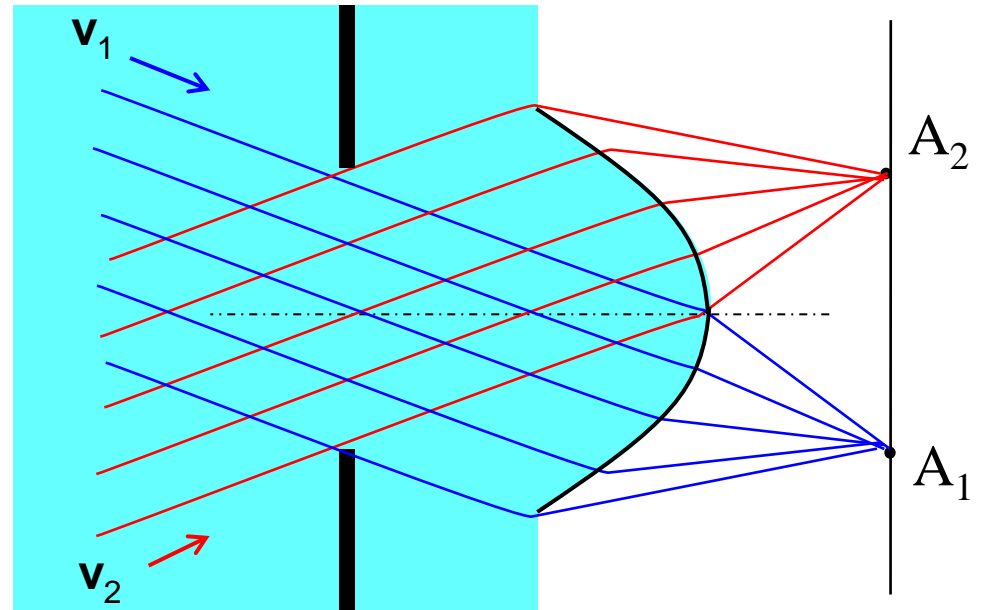
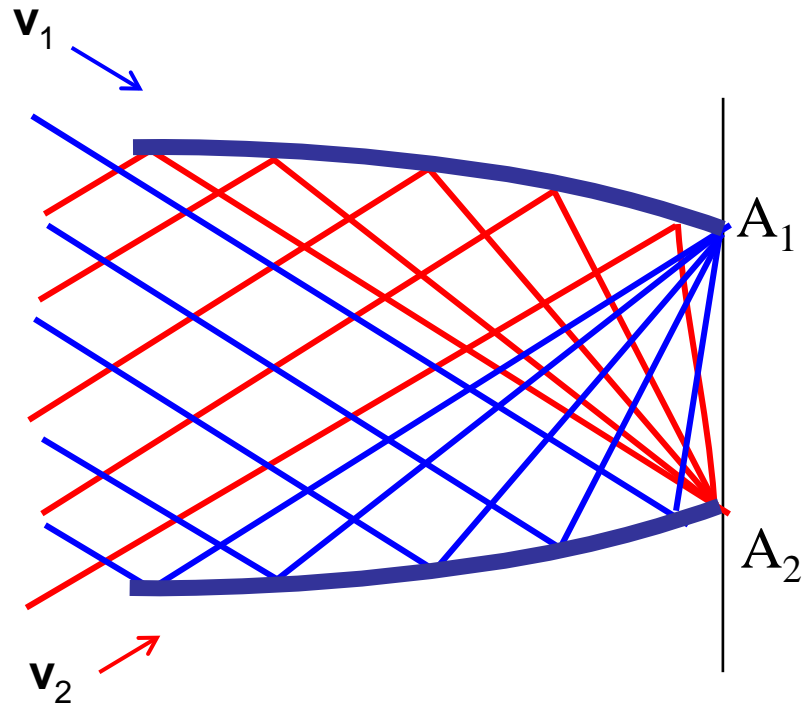
# One surface, two object points



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# One surface, two object points





# Early works

## On the problem of ideal flux concentrators

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a clue to another solution: if we have a surface in the system so placed that all the rays meet it on one side only of the axis, i.e., very remote from the aperture stop in ordinary lens design language, then this surface does not have to satisfy contradictory conditions and the edge-ray condition can be satisfied.

(1977)

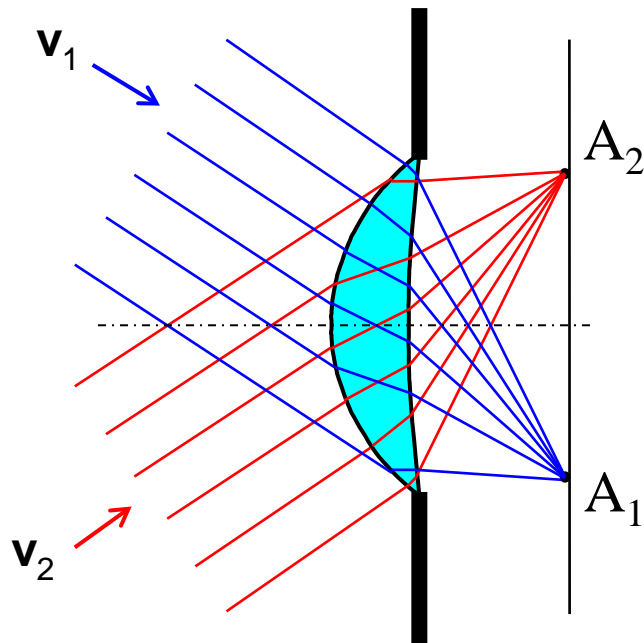


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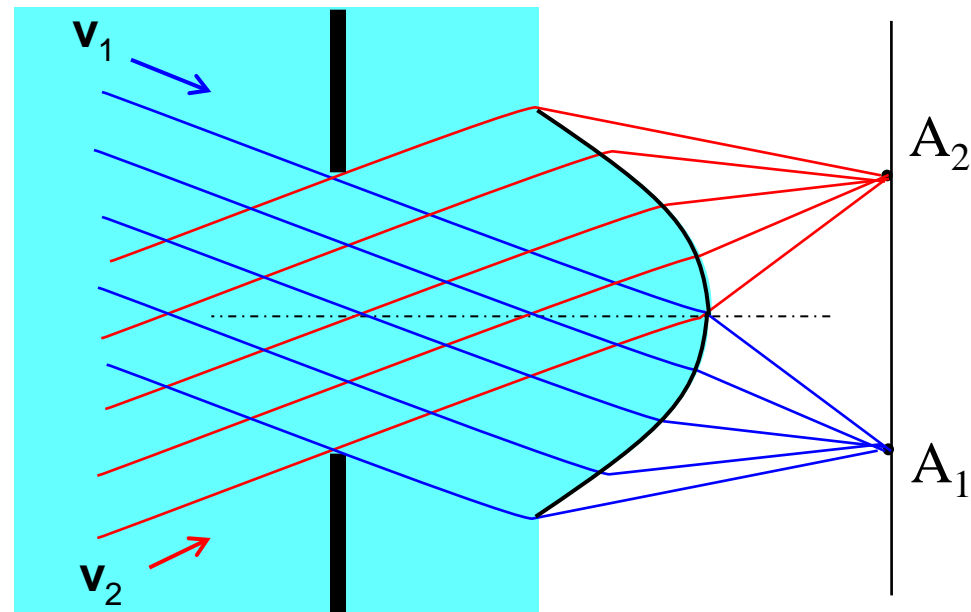


# Comparison

- Surfaces = beam print
- Two refractions

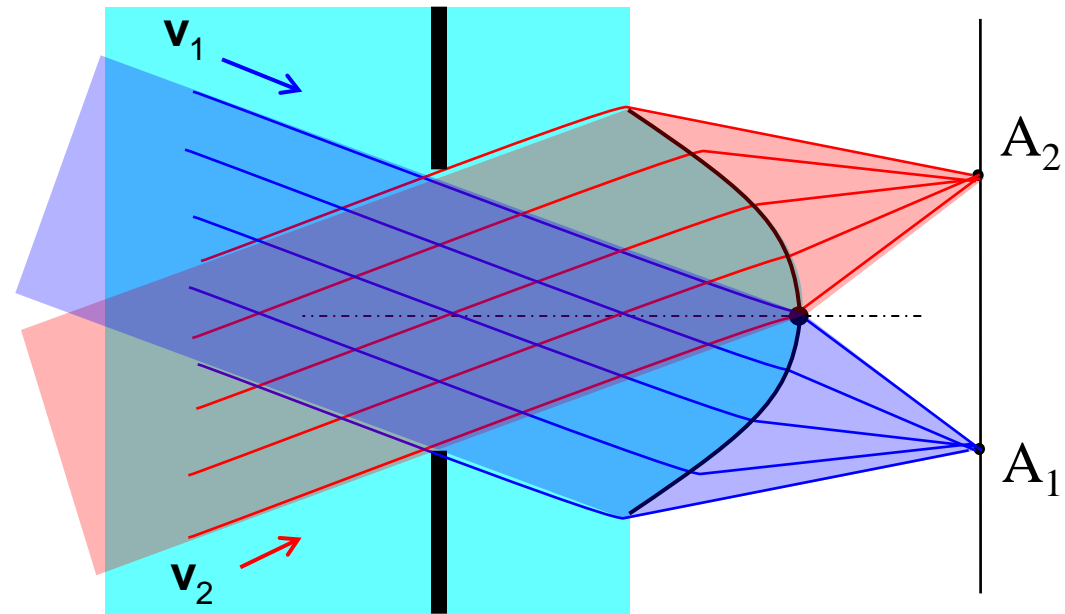
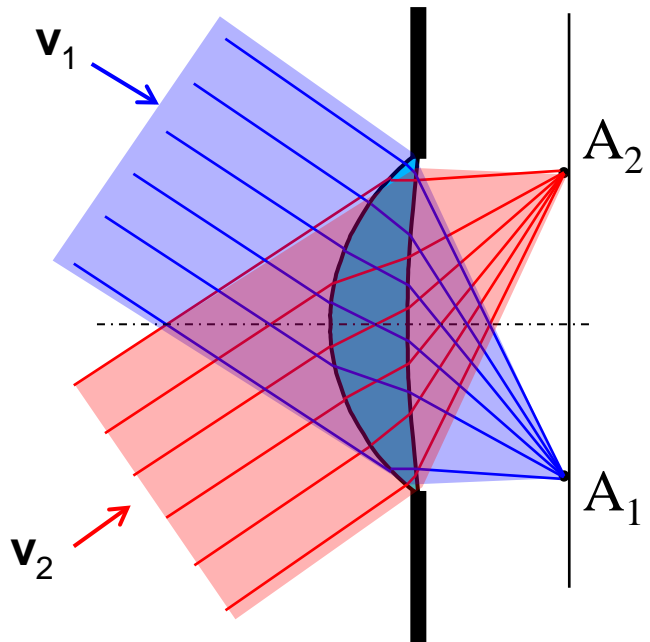
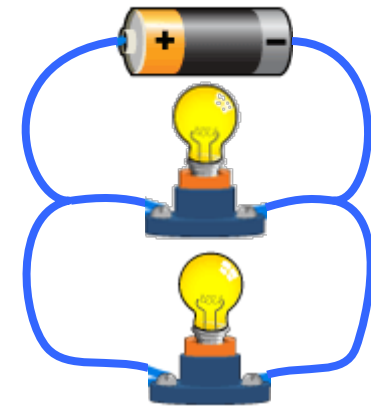
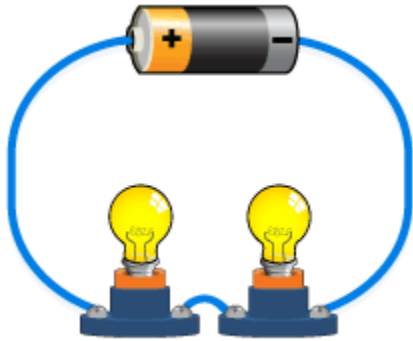


- Surface = 2 x beam print
- Single refraction



In both cases solutions are unique

# Comparison



Both cases can be also seen as two surfaces sharing one edge



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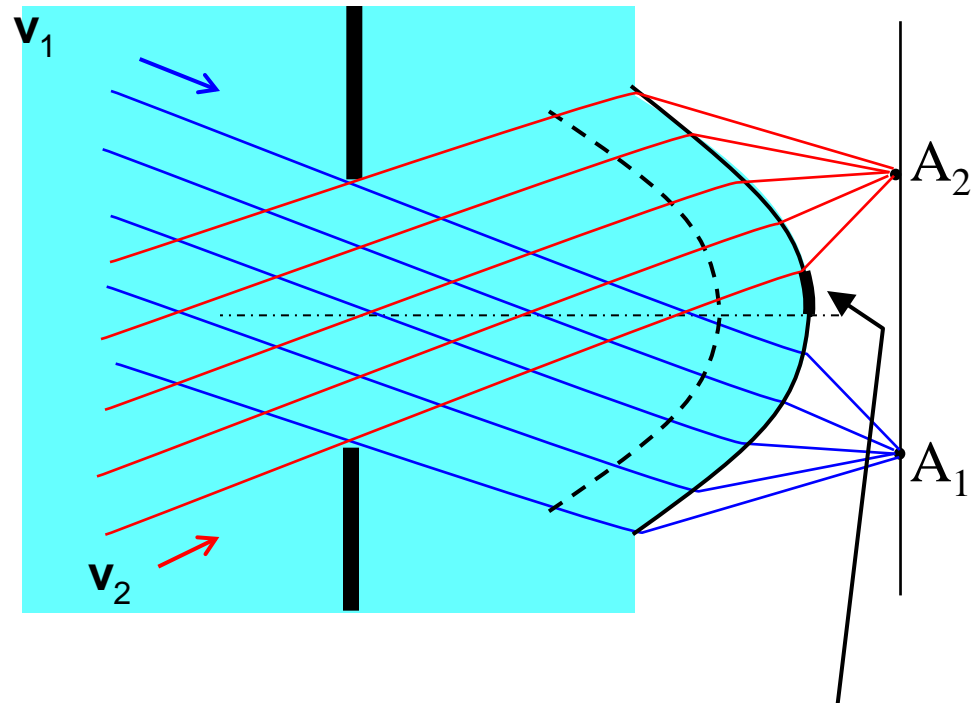
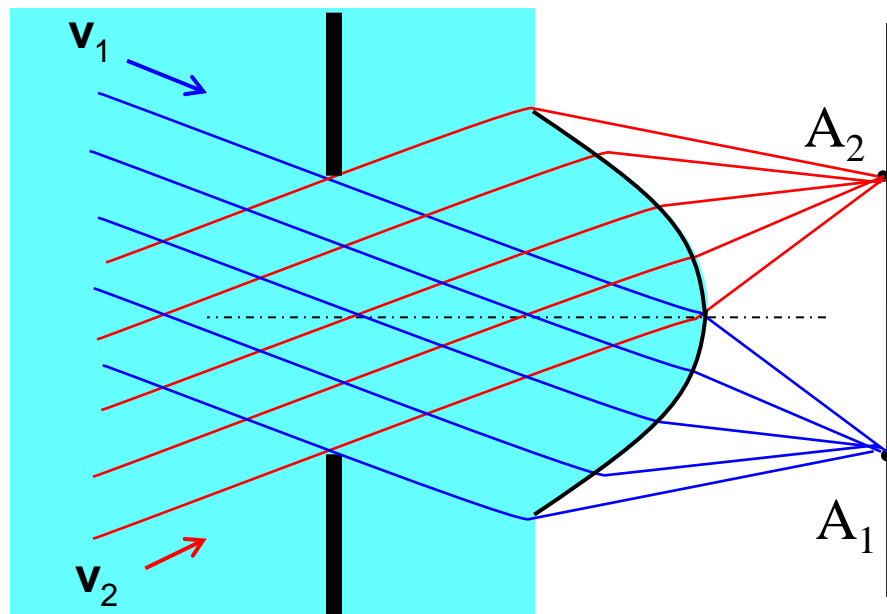


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# Increasing parallelism



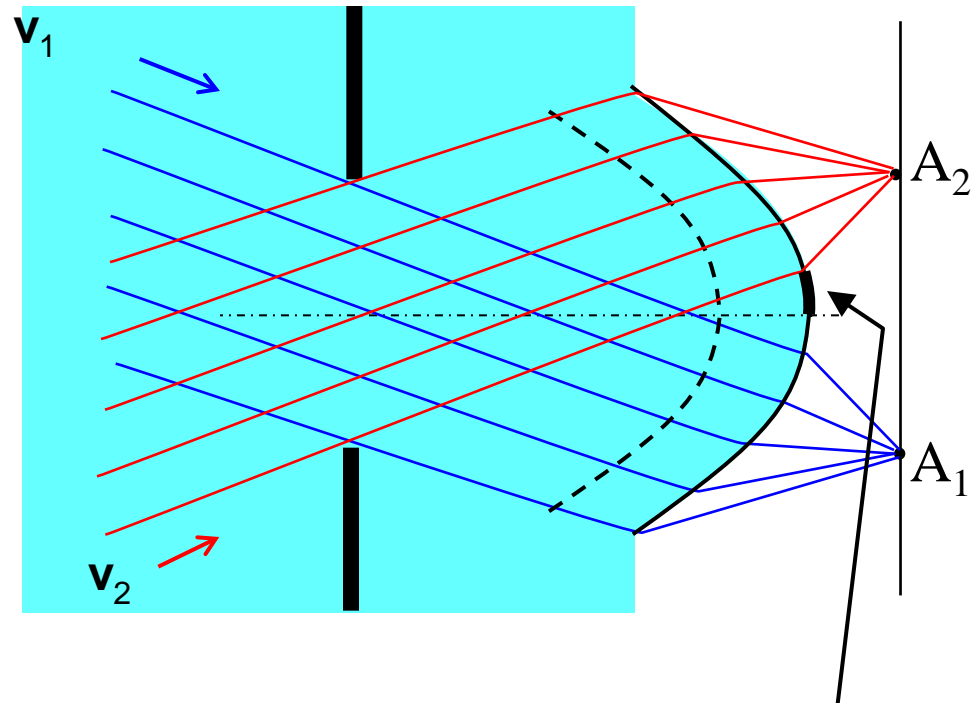
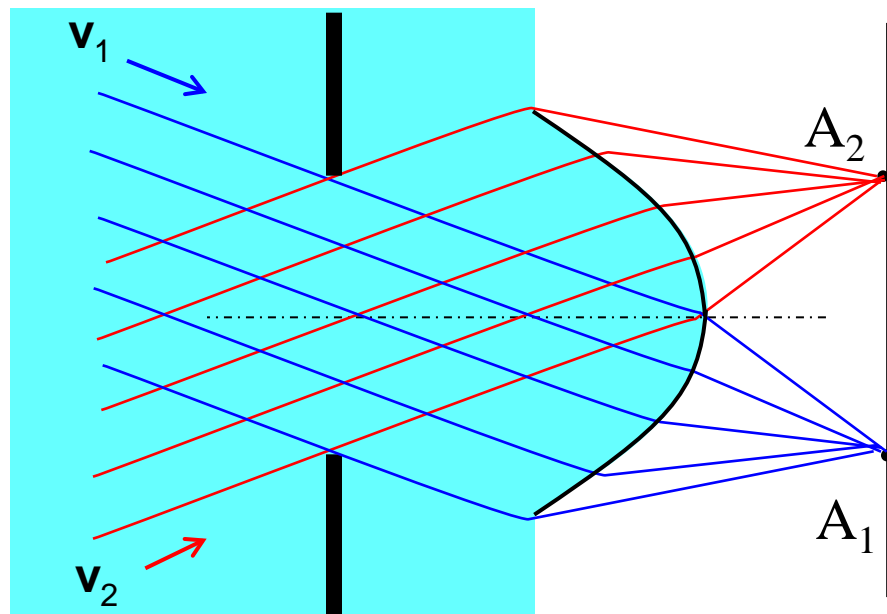
Free patch



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# Increasing parallelism



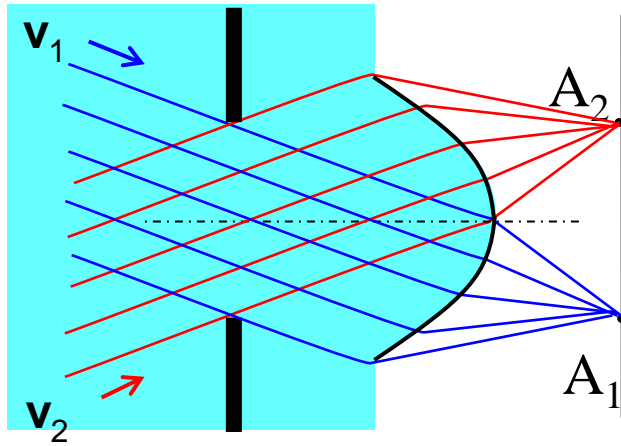
Free patch



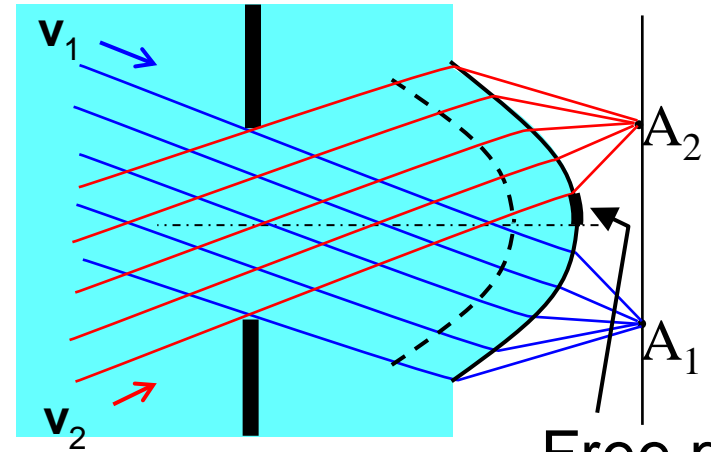
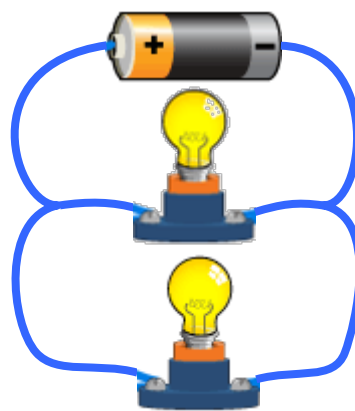
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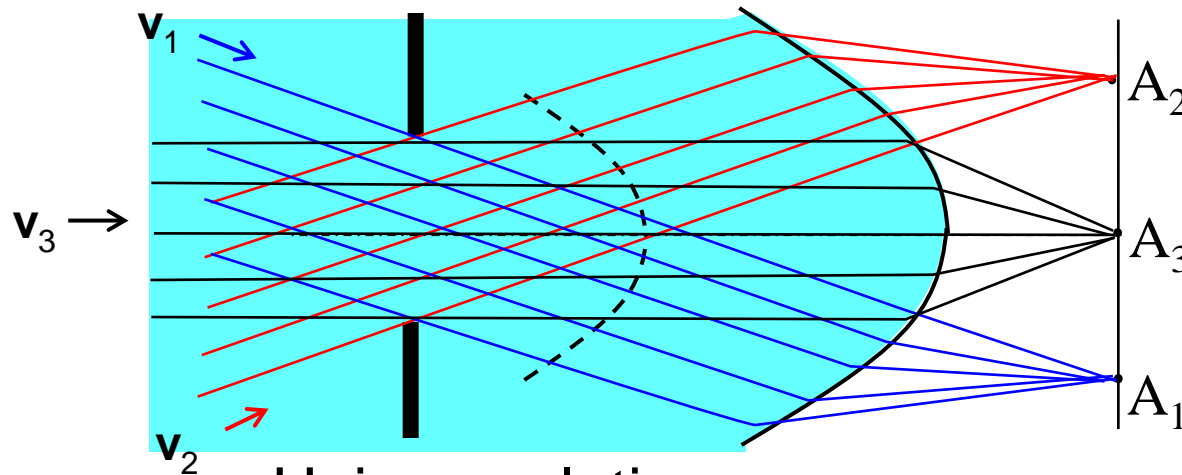
# Transition from two to three object points



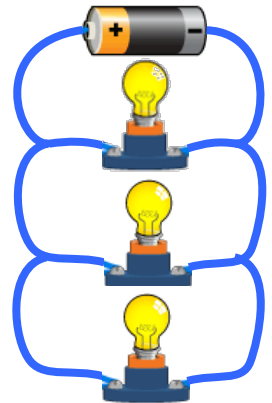
Unique solution



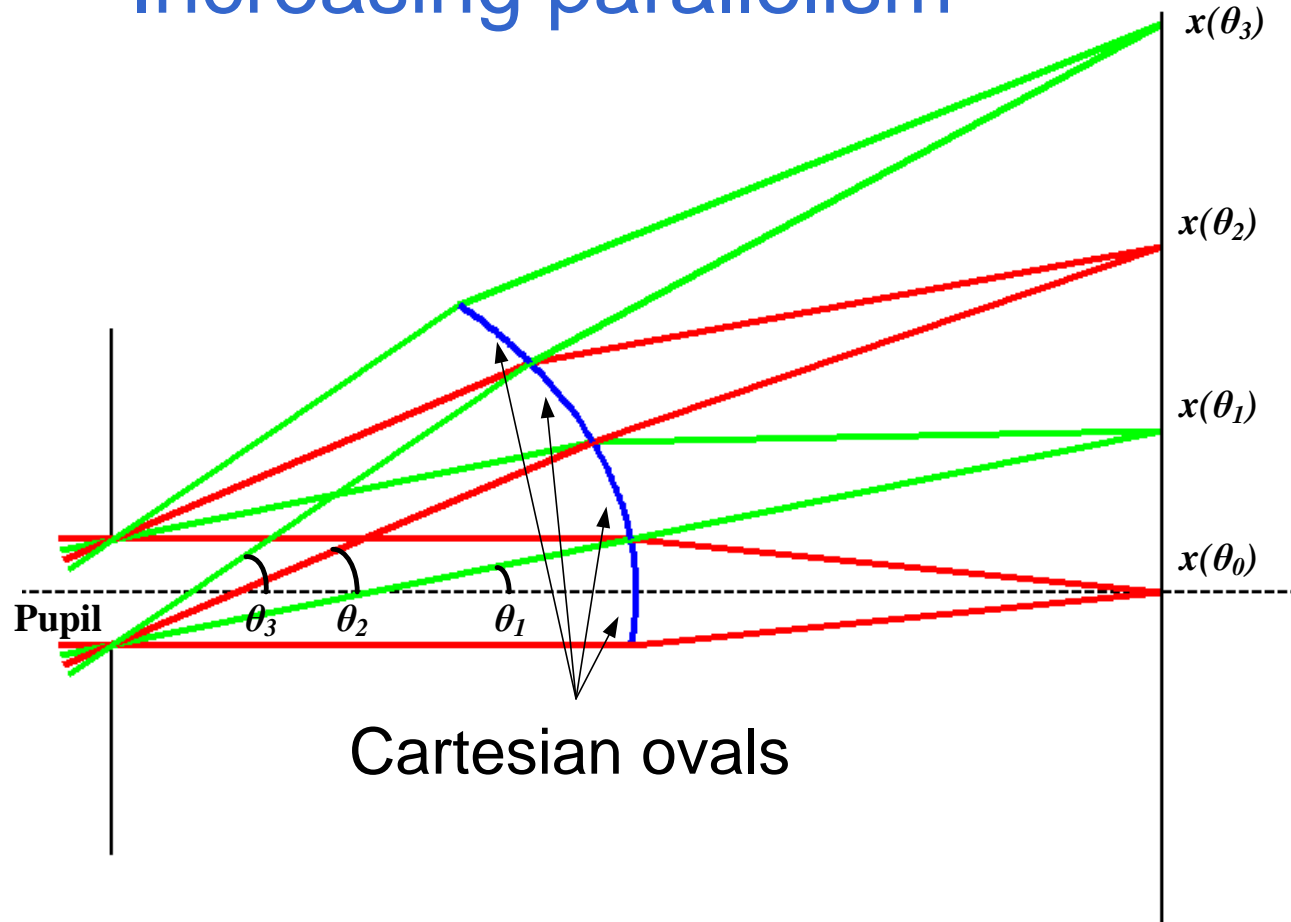
Free patch



Unique solution



# Increasing parallelism



L. Jiayao, P. Benítez, J.C. Miñano, SPIE Vol 8550, 2012

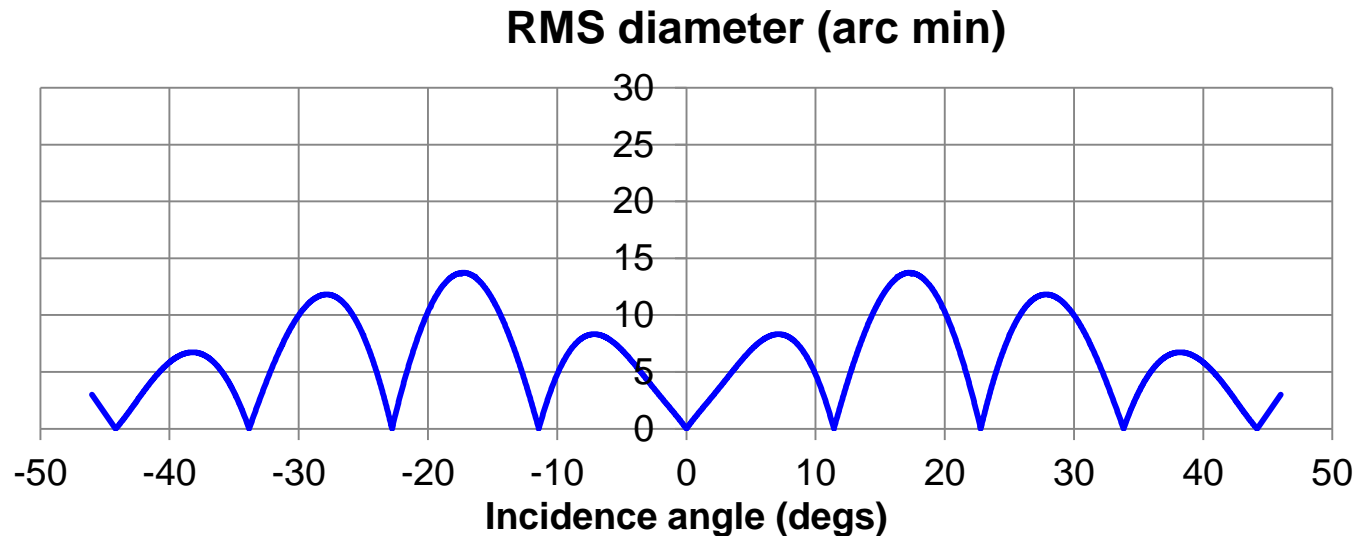


P. Benítez, J.C. Miñano, M. Nikolic,  
L. Jiayao, J.M. Infante, F. Duerr  
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# One surface, 10 object points



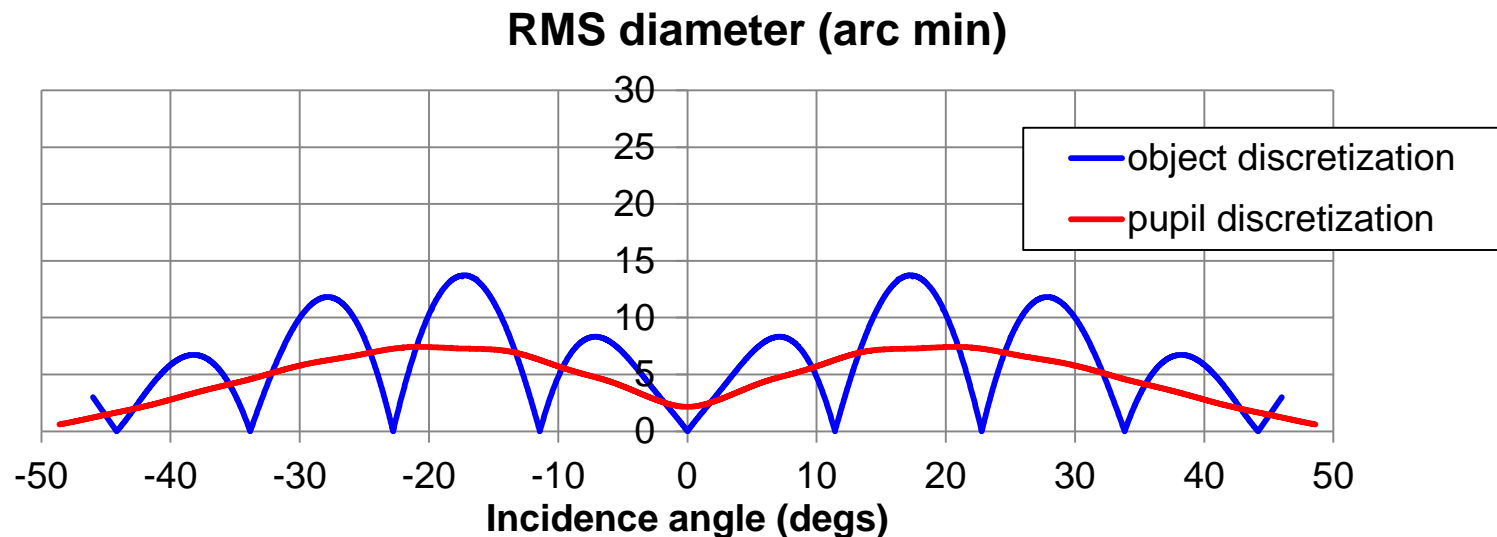
L. Jiayao, P. Benítez, J.C. Miñano, SPIE Vol 8550, 2012



P. Benítez, J.C. Miñano, M. Nikolic,  
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# One surface, 10 object points



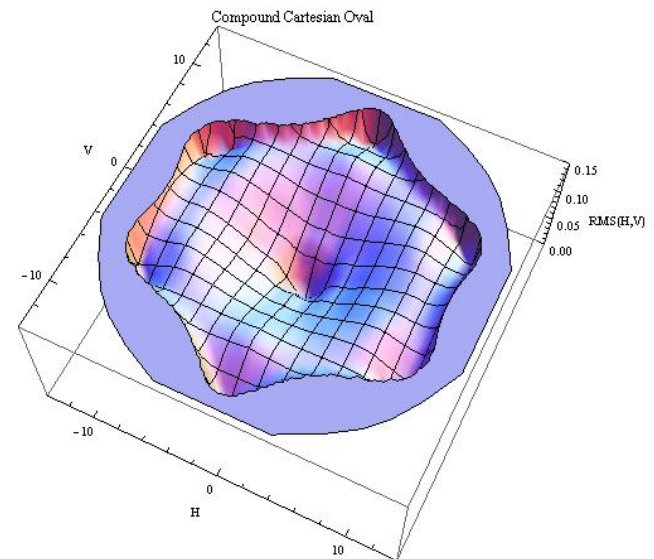
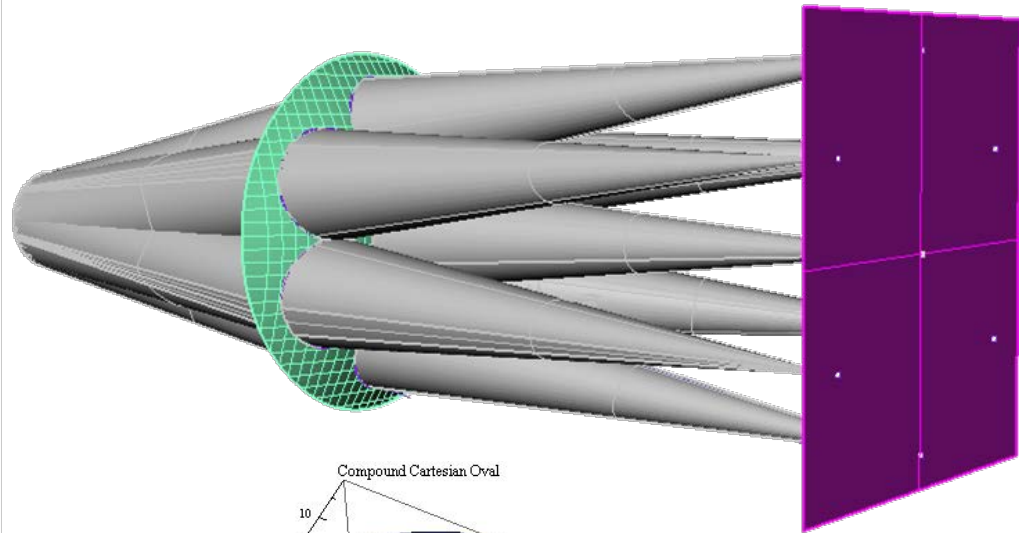
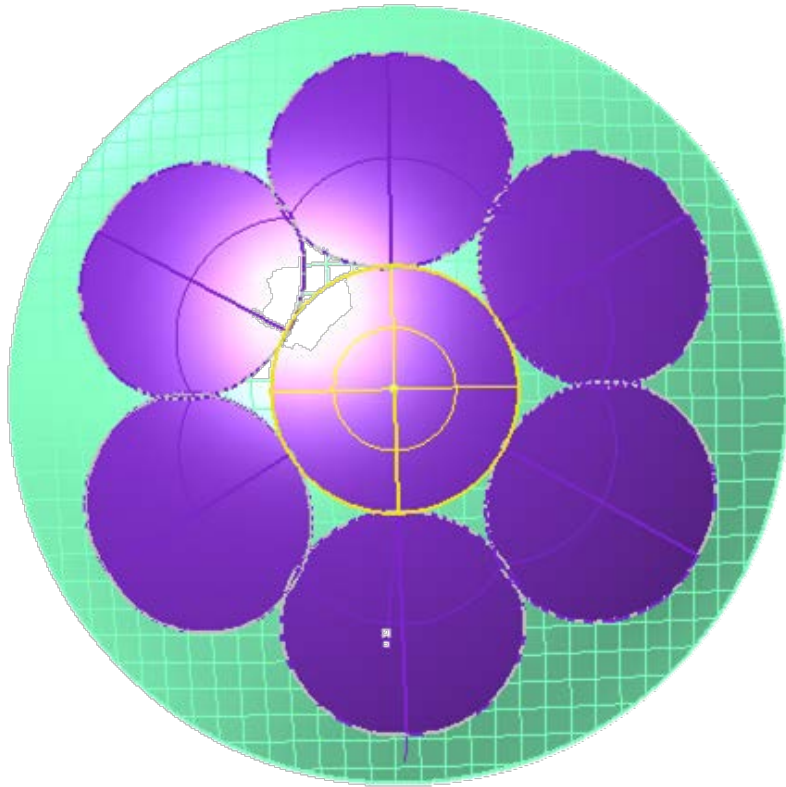
L. Jiayao, P. Benítez, J.C. Miñano, SPIE Vol 8550, 2012



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## Also in 3D

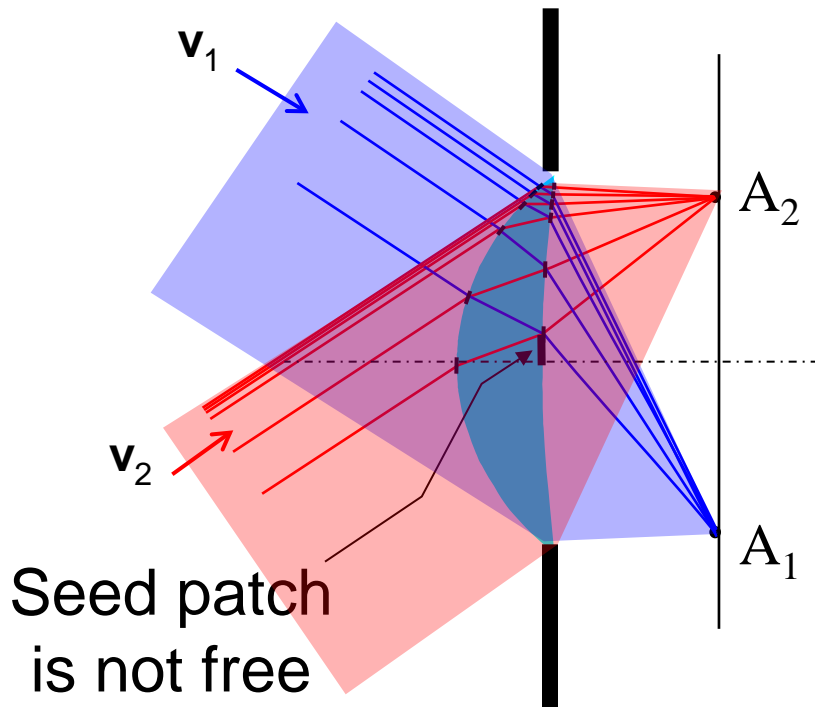


P. Benítez, J.C. Miñano, M. Nikolic,  
L. Jiayao, J.M. Infante, F. Duerr  
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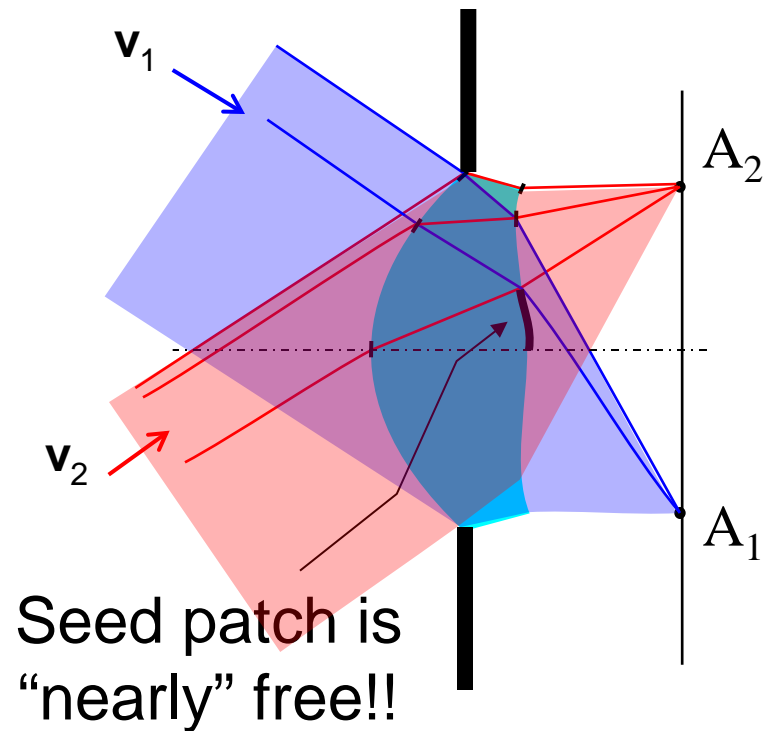


# Series-parallel combinations

SMS thicker lenses do not have convergence points



J.C. Miñano, J.C. Glez,  
Appl. Opt. 31 (16), 1992



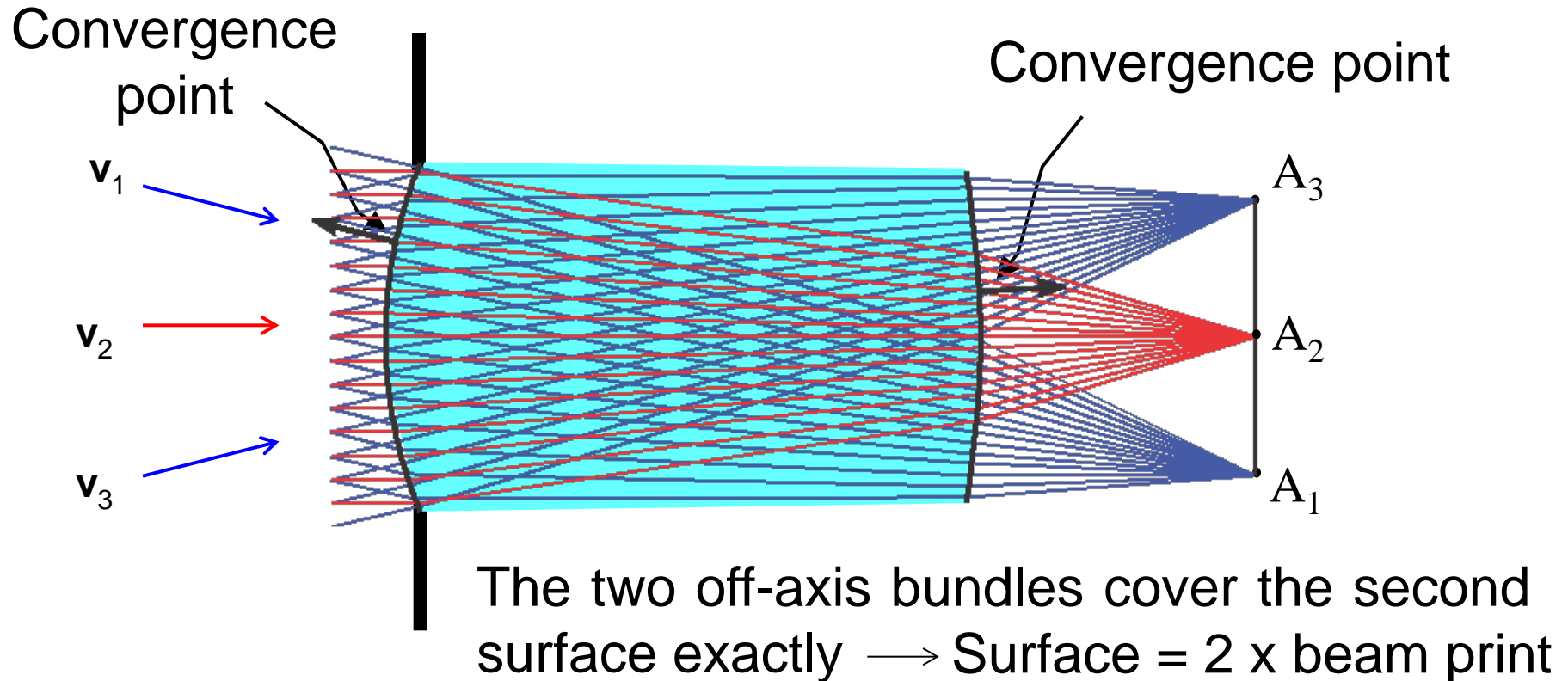
F. Muñoz P. Benítez, J.C. Miñano,  
SPIE Vol. 7061A 2008



P. Benítez, J.C. Miñano, M. Nikolic,  
L. Jiayao, J.M. Infante, F. Duerr  
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# Two surfaces, three object points



F. Duerr, P. Benítez, J.C. Miñano, Y. Meuret, H. Thienpont, Optics Express Vol. 20, No. 5, 2012

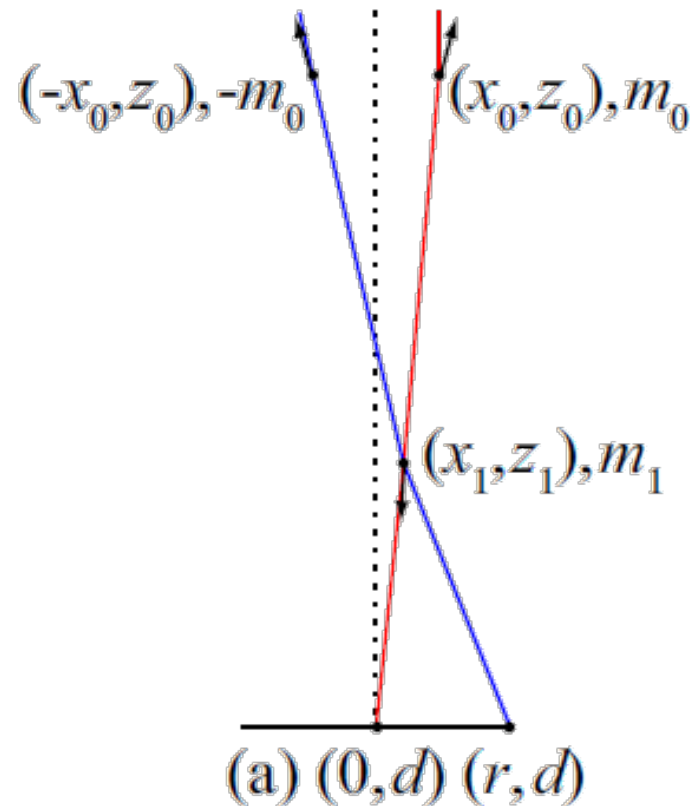
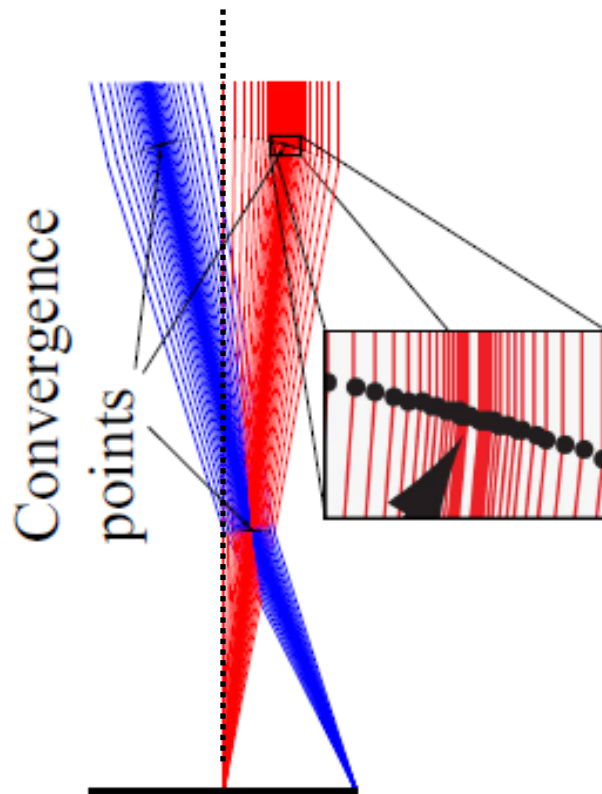
Unique analytic solution exists



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# Two surfaces, three object points



Unique analytic solution exists

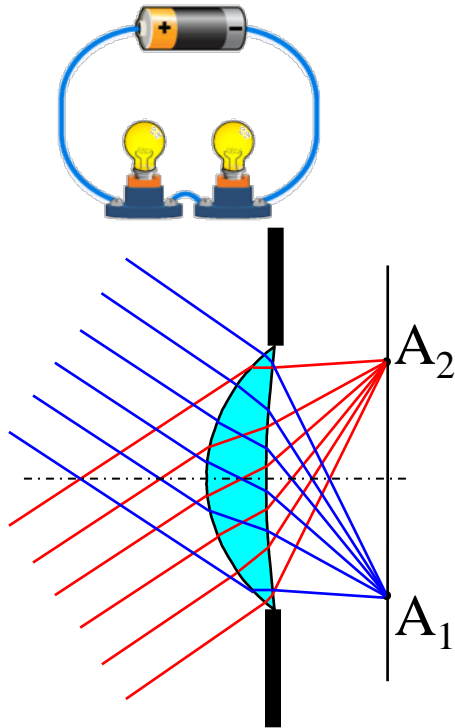
F. Duerr, P. Benítez, J.C. Miñano, Y. Meuret, H. Thienpont, Optics Express Vol. 20, No. 5, 2012



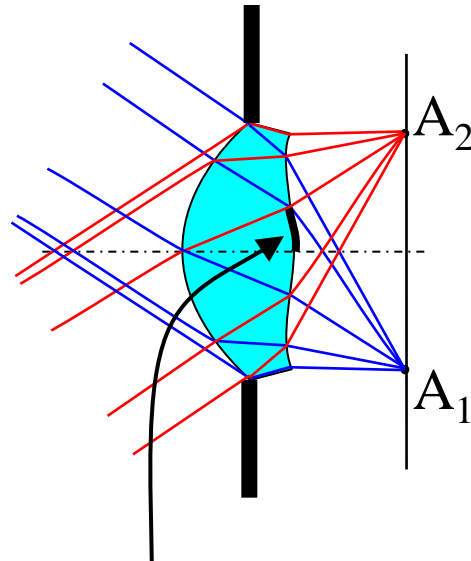
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# Transition from two to three object points

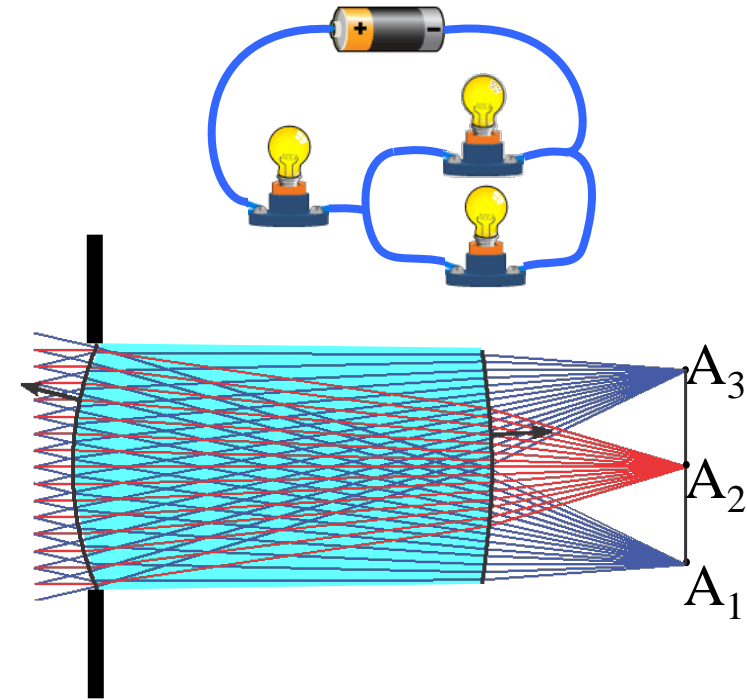


Unique solution



Free patch

Two object points



Unique solution

Three object points

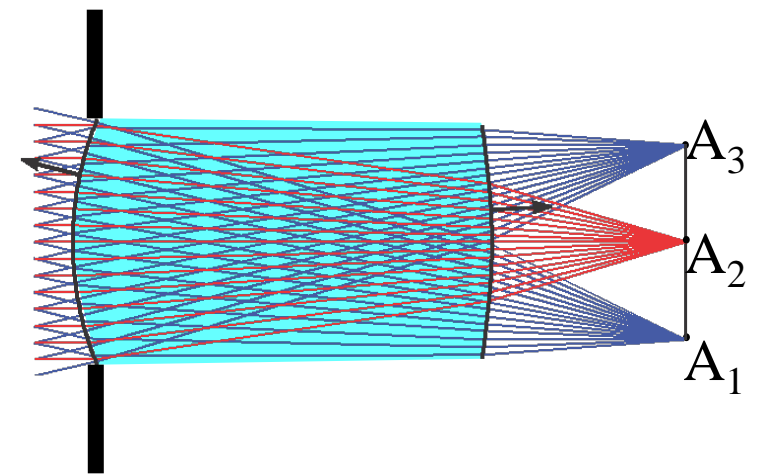
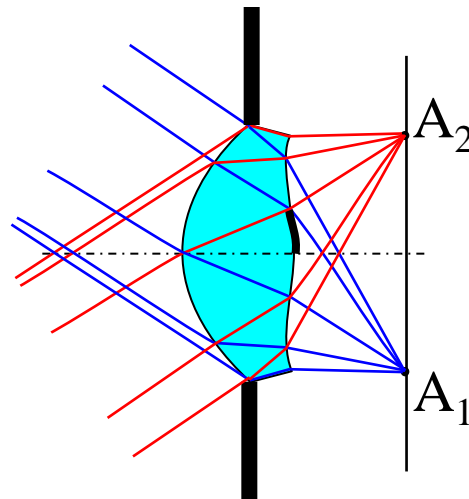
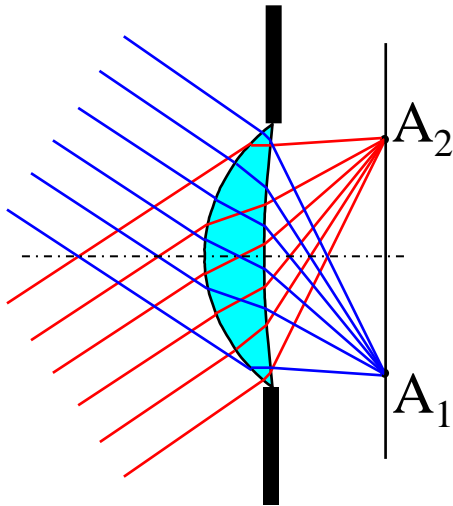
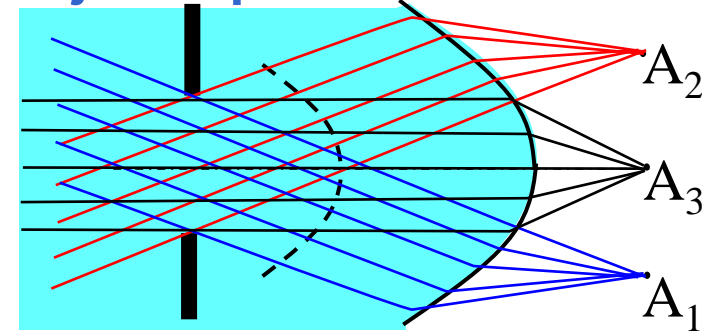
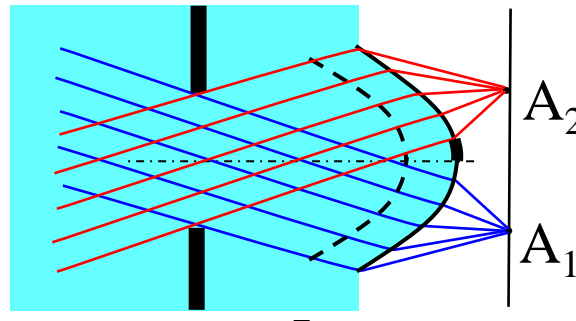
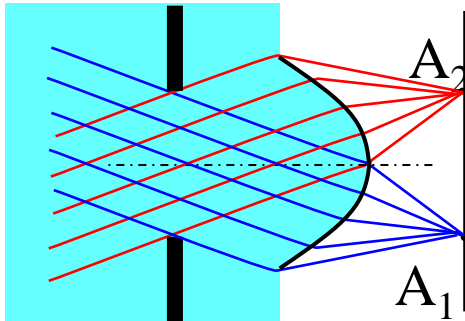


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# Transition from two to three object points



Unique solution

Free patch

Two object points

Unique solution  
Three object points



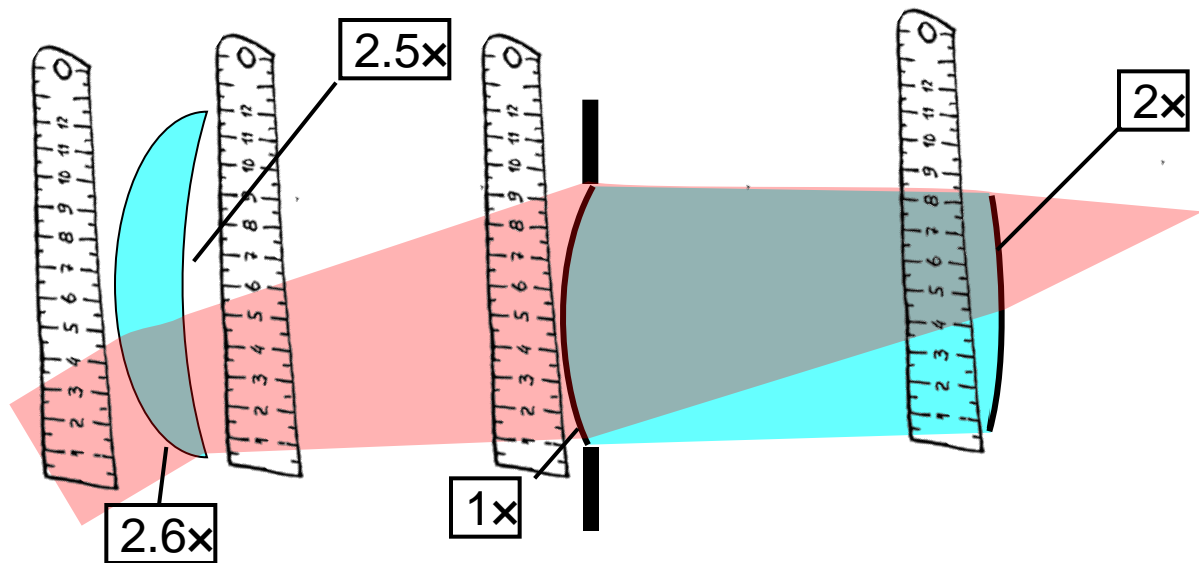
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# General rule of thumb

$$\text{Number of object points} \leq \sum E \left( \frac{\text{Extension of surface}}{\text{Extension of beam print}} \right)$$

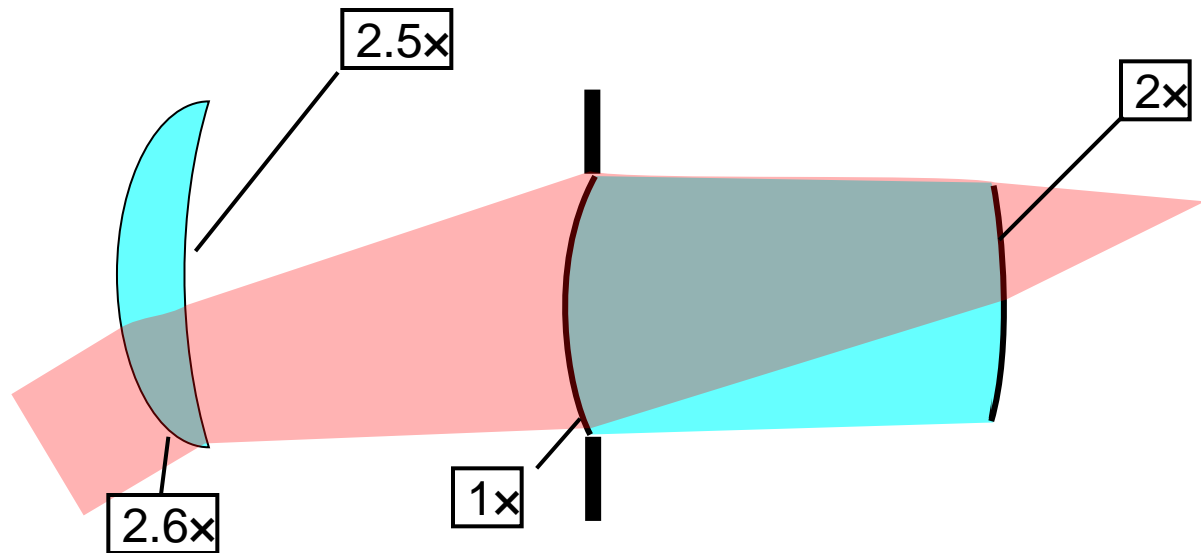


$$\text{Number of object points (2D)} \approx 2+2+1+2 = 7$$



# General rule of thumb

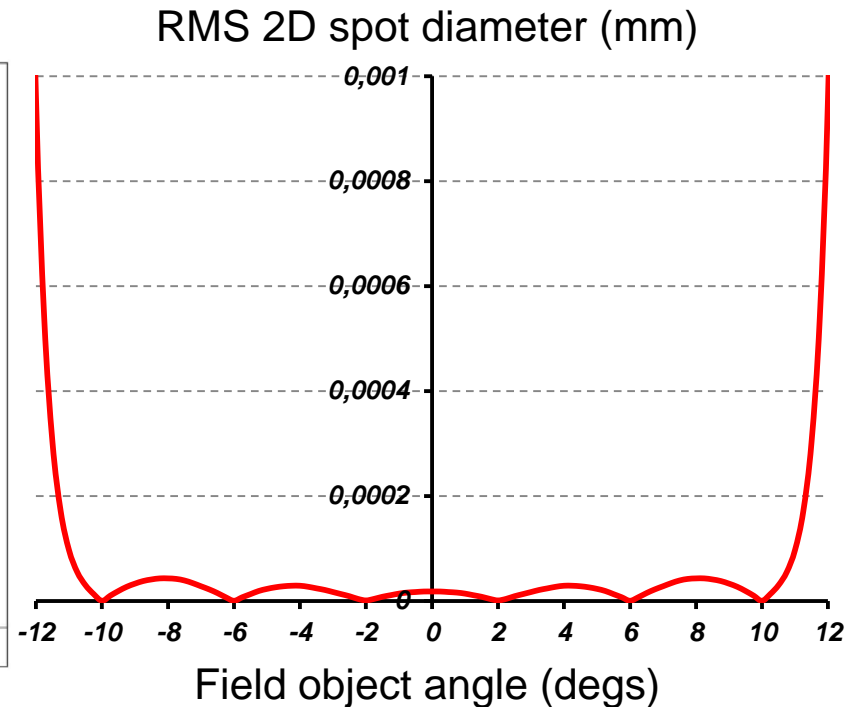
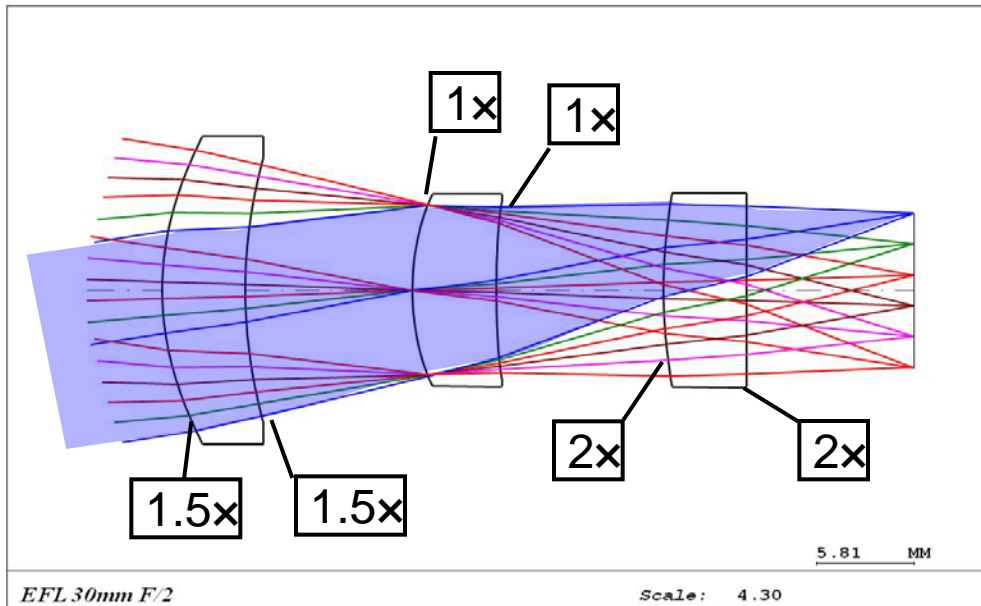
$$\text{Number of object points} \leq \sum \frac{\text{Extension of surface}}{\text{Extension of beam print}}$$



$$\text{Number of object points (3D; round field)} \approx 2^2 + 2^2 + 1^2 + 2^2 = 13$$

# Example

First design: 6 surfaces, 6 object points



$$1+1+1+1+2+2 = 8$$

Jose Infante, PhD dissertation, October 2013

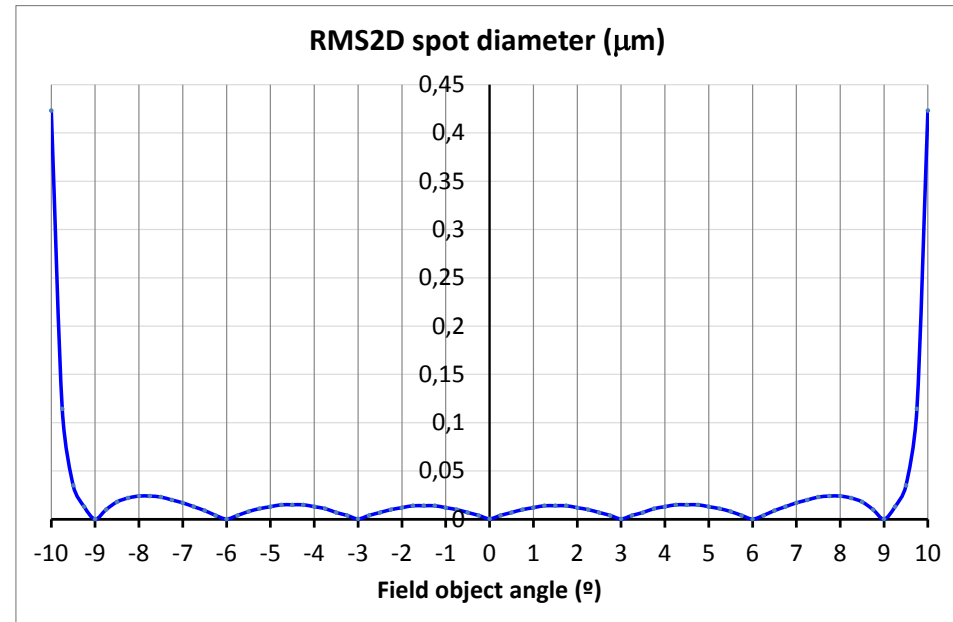
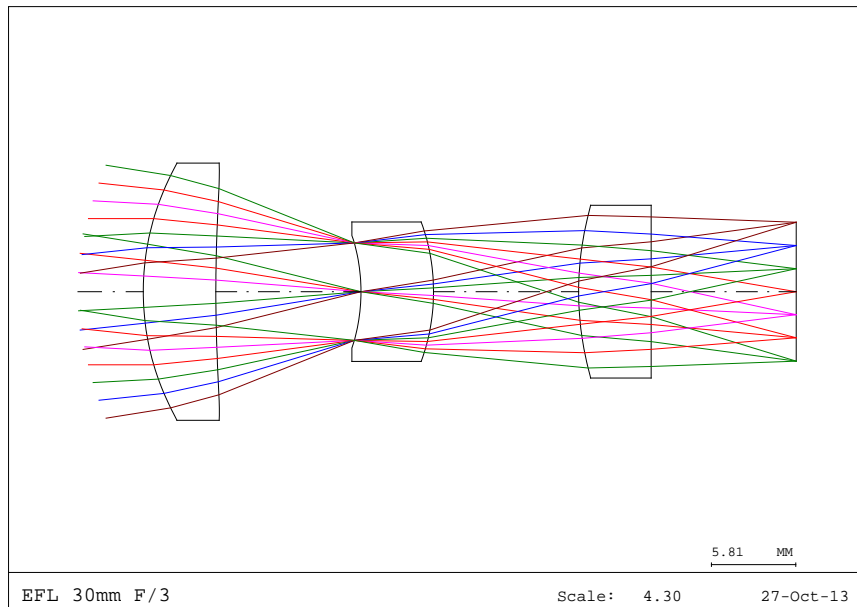


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# Example

Improved design: 6 surfaces, 7 object points



Still improvable!

$$1+1+1+1+2+2 = 8$$

8 zeros should be achievable!



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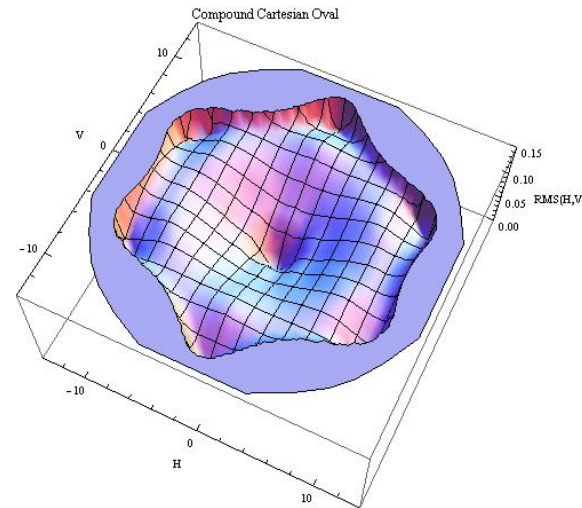
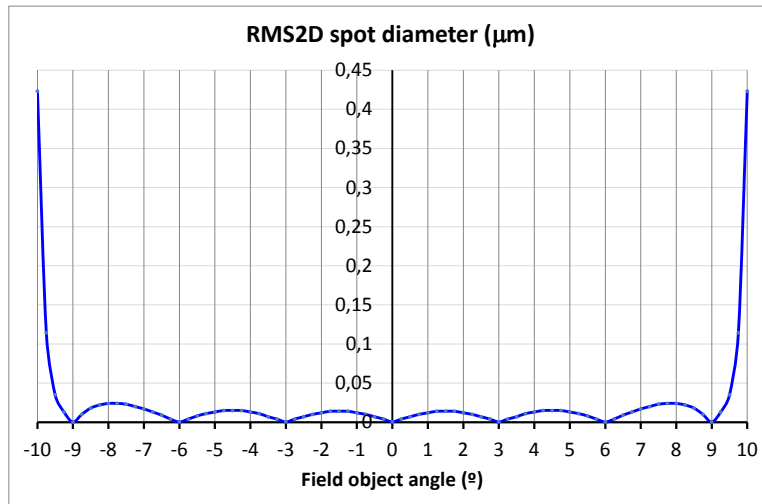
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# SMS and optimization combination

When maximizing the object points to sharp image, we try to exhaust the degrees of freedom of aspherics and freeforms.



We conjecture that maximal SMS designs are close to a good solution (local minimum)



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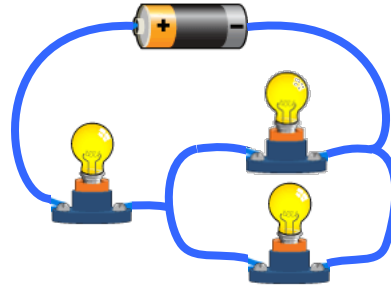


# SMS optimization strategies

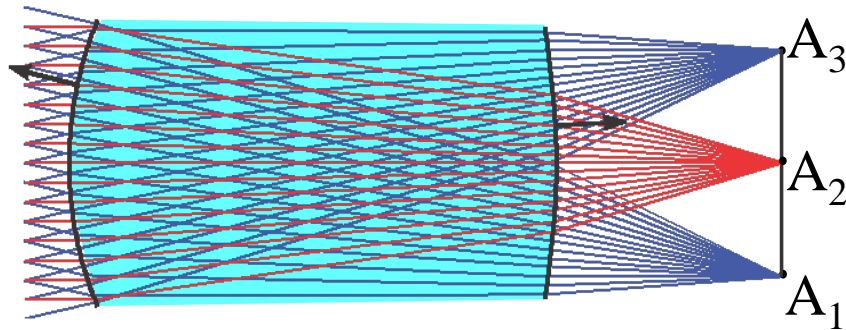
1. SMS surface can be combined with standard surfaces.
2. The free-parameters of the SMS (vertices positions, free patches, wavefronts) can be optimised.
3. An SMS design can be used as a good starting point for a standard optimization



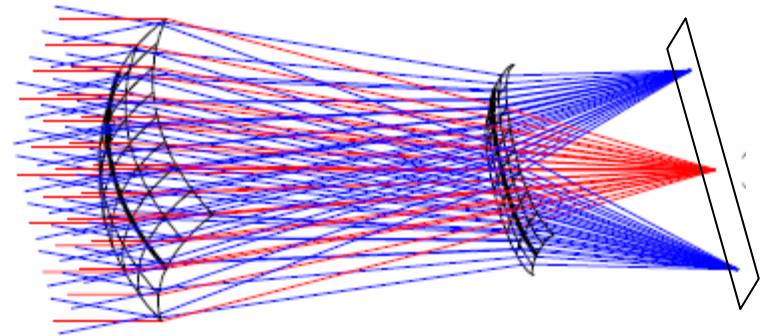
# Example: Imaging with high aspect ratio



SMS 2D



SMS 3D



F. Duerr, P. Benítez, J.C. Miñano, Y. Meuret, H. Thienpont, Opt.Express 20,1 5576–5585, (2012)

F. Duerr, P. Benítez, J.C. Miñano, Y. Meuret, H. Thienpont, Optics Express 20, 10839–10846, (2012)

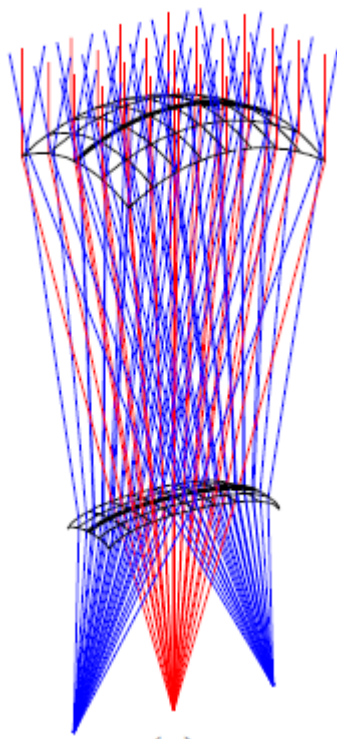


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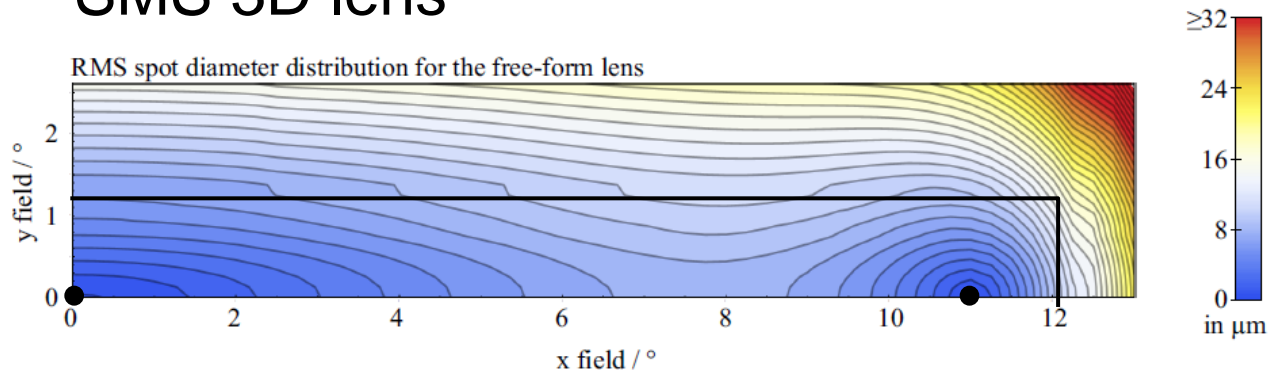




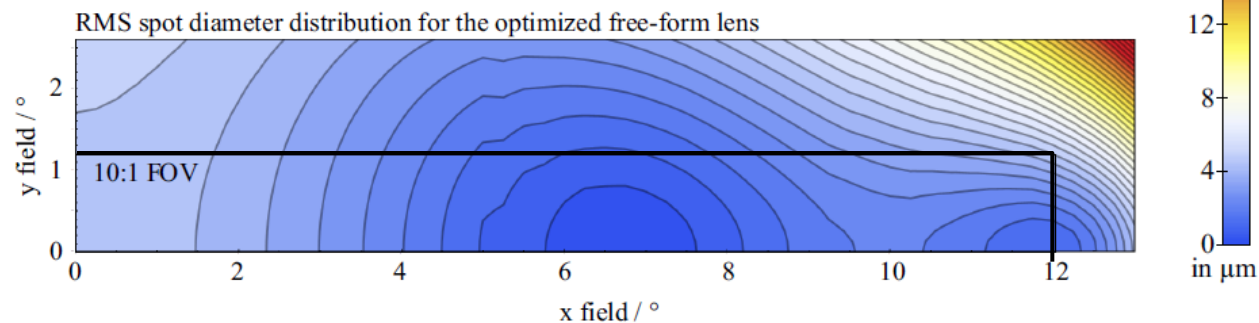
# Imaging with high aspect ratio



## SMS 3D lens



## SMS 3D lens + optimization



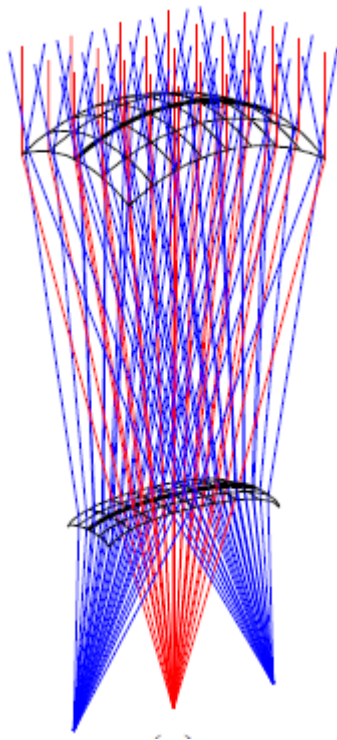
F.Duerr, P. Benítez, J.C. Miñano, Y. Meuret, H. Thienpont, Optics Express 20, 20,10839–10846 (2012)



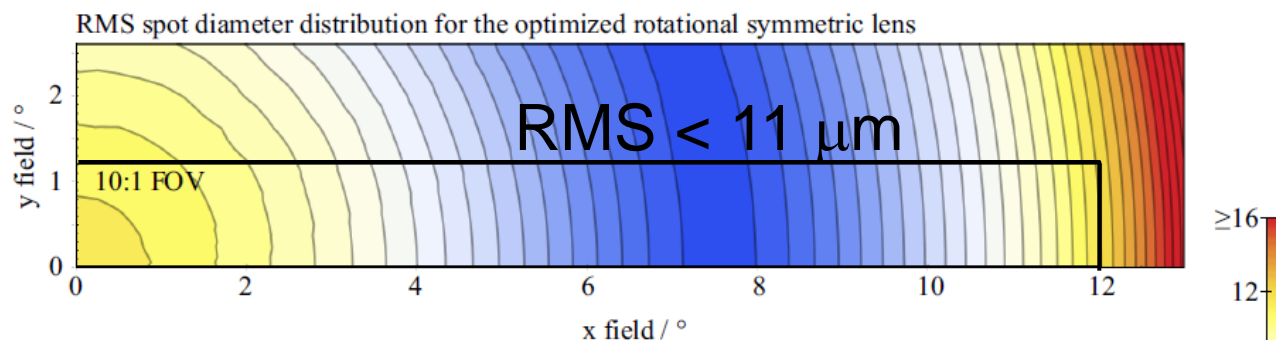
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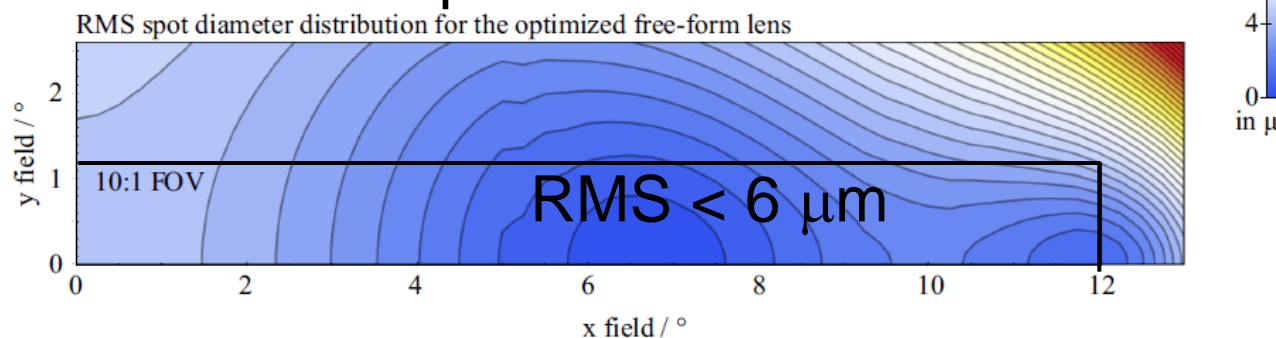
# Imaging with high aspect ratio



## Optimised rotational lens



## SMS lens + optimization



F.Duerr, P. Benítez, J.C. Miñano, Y. Meuret, H. Thienpont, Optics Express 20, 20,10839–10846 (2012)



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# Conclusions

- Is it possible to sharply image  $M$  object points with  $N$  surfaces when  $N < M$ ? **Yes!**
- Under what conditions? **When surfaces are not at the aperture stop.**
- Why is it interesting for optimization? **You have an good starting point**
- What is the role of the SMS method? **Provides a direct algorithm to the solution**



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The Universidad Politécnica de Madrid (UPM) thanks:

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Thank you!



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